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FINAL JEE-MAIN EXAMINATION - JULY, 2022 (Held On Friday 29th July, 2022) TIME: 3:00 PM to 06:00 PM PHYSICS TEST PAPER WITH SOLUTION **SECTION-A** Choose the correct answer from the options given Two identical metallic spheres A and B when 1. below: placed at certain distance in air repel each other (A) A-III, B-II, C-I, D-IV with a force of F. Another identical uncharged sphere C is first placed in contact with A and then (B) A-III, B-IV, C-II, D-I in contact with B and finally placed at midpoint (C) A-IV, B-I, C-III, D-II between spheres A and B. The force experienced (D) A-II, B-III, C-I, D-IV by sphere C will be : (A) 3F/2(B) 3F/4 Official Ans. by NTA (B) (C) F (D) 2F Official Ans. by NTA (B) Nm Sol. Torque =  $F \times r_{\perp}$ **Sol.** Let  $q_A = q_B = q$ Stress =  $\frac{\text{Force}}{\text{Area}}$  $N/m^2$ (A) (B)  $F = \frac{Kq^2}{r^2}$ Latent heat =  $\frac{\text{Energy}}{\text{Mass}}$ J Kg<sup>-1</sup> When C is placed in contact with A, charge on A & C will be =  $\frac{q}{2}$ Power =  $\frac{\text{Work}}{\text{Time}}$  $N ms^{-1}$ Now C is placed in contact with B, charge on B & A-III, B-IV, C-II, D-I C will be =  $\frac{q + \frac{q}{2}}{2} = \frac{3q}{4}$ Two identical thin metal plates has charge  $q_1$  and  $q_2$ 3. Now. respectively such that  $q_1 > q_2$ . The plates were brought close to each other to form a parallel plate  $\frac{\mathbf{q}}{\mathbf{2}} \bigtriangleup \begin{array}{c} F_1 & F_2 \\ \hline F_1 & F_2 \\ \hline F_2 & F$ capacitor of capacitance C. The potential difference between them is : (A)  $\frac{\left(q_1+q_2\right)}{C}$  (B)  $\frac{\left(q_1-q_2\right)}{C}$  $F' = F_2 - F_1 = \frac{\left(K\frac{3q}{4} - K\frac{q}{2}\right)}{\frac{r^2}{4}} \cdot \frac{3q}{4}$ (C)  $\frac{(q_1 - q_2)}{2C}$  (D)  $\frac{2(q_1 - q_2)}{C}$  $=\frac{3Kq^2}{4r^2}=\frac{3F}{4}$  (B) Official Ans. by NTA (C) 2. Match List I with List II. **Sol.** Electric field between plates  $E = \frac{q_1 - q_2}{2A \epsilon_0}$ List I List II A. Torque I. Nms<sup>-1</sup>  $J kg^{-1}$  $V = Ed = \frac{q_1 - q_2}{2A \in_0} d$ B. II. Stress Latent C. Heat III. Nm  $V = \frac{q_1 - q_2}{2C}$ IV.  $Nm^{-2}$ D. Power



Given below are two statements: one is labelled as
Assertion A and the other is labelled as Reason R.
Assertion A: Alloys such as constantan and manganin are used in making standard resistance coils.

**Reason R:** Constantan and manganin have very small value of temperature coefficient of resistance.

In the light of the above statements, choose the correct answer from the options given below.

- (A) Both A and R are true and R is the correct explanation of A.
- (B) Both A and R are true but R is NOT the correct explanation of A.
- (C) A is true but R is false.
- (D) A is false but R is true.

Official Ans. by NTA (A)

Sol. Theory based

5. A 1 m long wire is broken into two unequal parts X and Y The X part of the wire is streched into another wire W. Length of W is twice the length of X and the resistance of W is twice that of Y. Find the ratio of length of X and Y.

(B) 1 : 2

(D) 2:1

(A)1:4

Official Ans. by NTA (B)

Sol. 
$$\begin{pmatrix} \ell & 1-\ell \\ \hline & 0 & 0 \\ \hline & X & Y \\ \hline & 2\ell \\ \hline & W \\ \end{bmatrix}$$

$$\frac{\mathbf{R}_{\mathbf{X}}}{\mathbf{R}_{\mathbf{Y}}} = \frac{\ell_{\mathbf{X}}}{\ell_{\mathbf{Y}}}$$

When wire is stretched to double of its length, then resistance becomes 4 times

$$R_{W} = 4R_{X} = 2R_{Y}$$
$$\frac{R_{X}}{R_{Y}} = \frac{1}{2}$$
So.  $\frac{\ell_{X}}{\ell} = \frac{1}{2}$ 

6. A wire X of length 50 cm carrying a current of 2 A is placed parallel to a long wire Y of length 5 m. The wire Y carries a current of 3 A. The distance between two wires is 5 cm and currents flow in the same direction. The force acting on the wire Y is :

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$$2A$$
  $4$   $3A$   $3A$ 

(A)  $1.2 \times 10^{-5}$  N directed towards wire X. (B)  $1.2 \times 10^{-4}$  N directed away from wire X. (C)  $1.2 \times 10^{-4}$  N directed towards wire X. (D)  $2.4 \times 10^{-5}$  N directed towards wire X. Official Ans. by NTA (A)

**Sol.** Force of interaction =  $I_1 \ell_1 B_{12}$ 

$$= \frac{\mu_0 I_1 I_2}{2\pi r} \ell_1$$
$$= \frac{4\pi \times 10^{-7} \times 6 \times 0.5}{2\pi \times 5 \times 10^{-2}}$$
$$= 1.2 \times 10^{-5} \text{ towards X}$$

A juggler throws balls vertically upwards with same initial velocity in air. When the first ball reaches its highest position, he throws the next ball. Assuming the juggler throws n balls per second, the maximum height the balls can reach is

**Sol.** Time taken by ball to reach highest point  $= \frac{u}{g}$ 

Frequency of throw  $= \frac{g}{u} = n$ 

$$\Rightarrow u = \frac{g}{n}$$

$$H_{max} = \frac{u^2}{2g} = \frac{\left(\frac{g}{n}\right)^2}{2g}$$

$$\frac{g}{2n^2}$$

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7.

8. A circuit element X when connected to an a.c. supply of peak voltage 100 V gives a peak current of 5 A which is in phase with the voltage. A second element Y when connected to the same a.c. supply also gives the same value of peak current which lags behind the voltage by  $\frac{\pi}{2}$ . If X and Y are connected in series to the same supply, what will be the rms value of the current in ampere ?

(A) 
$$\frac{10}{\sqrt{2}}$$
 (B)  $\frac{5}{\sqrt{2}}$  (C)  $5\sqrt{2}$  (D)  $\frac{5}{2}$ 

Official Ans. by NTA (D)

Sol. Element X should be resistive with  $R = 20\Omega$ Element Y should be inductive with  $X_L = 20 \Omega$ When X and Y are connector in series

$$Z = \sqrt{X_{L}^{2} + R^{2}} = 20\sqrt{2}$$
$$I_{0} = \frac{E_{0}}{Z} = \frac{100}{20\sqrt{2}} = \frac{5}{\sqrt{2}} A$$
$$I_{rms} = \frac{I_{0}}{\sqrt{2}} = \frac{5}{2} A$$

9. An unpolarised light beam of intensity  $2I_0$  is passed through a polaroid P and then through another polaroid Q which is oriented in such a way that its passing axis makes an angle of 30° relative to that of P. The intensity of the emergent light is

(A) 
$$\frac{I_0}{4}$$
 (B)  $\frac{I_0}{2}$  (C)  $\frac{3I_0}{4}$  (D)  $\frac{3I_0}{2}$ 

Official Ans. by NTA (C)

Sol.  

$$I_{1} = \frac{1}{2}(2I_{0}) = I_{0}$$

$$I_{2} = I_{1} \cos^{2} 30^{\circ}$$

$$-I_{0} = \frac{3}{2} - \frac{3I_{0}}{2}$$

10. An  $\alpha$  particle and a proton are accelerated from rest through the same potential difference. The ratio of linear momenta acquired by above two particals will be :

> (A)  $\sqrt{2}$  : 1 (B)  $2\sqrt{2}$  : 1 (C)  $4\sqrt{2}$  : 1 (D) 8 : 1

Official Ans. by NTA (B)

Sol. 
$$p = \sqrt{2mE} = \sqrt{2mqV}$$
  
 $\frac{p_{\alpha}}{p_{p}} = \sqrt{\frac{m_{\alpha}q_{\alpha}}{m_{p}q_{p}}} = \sqrt{\frac{4}{1} \times \frac{2}{1}}$   
 $2\sqrt{2}$ 

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- **11.** Read the following statements:
  - (A) Volume of the nucleus is directly proportional to the mass number.
  - (B) Volume of the nucleus is independent of mass number.
  - (C) Density of the nucleus is directly proportional to the mass number.
  - (D) Density of the nucleus is directly proportional to the cube root of the mass number.
  - (E) Density of the nucleus is independent of the mass number.

Choose the correct option from the following options.

(A) (A) and (D) only.
(B) (A) and (E) only.
(C) (B) and (E) only.
(D) (A) and (C) only
Official Ans. by NTA (B)

Sol. 
$$R \propto A^{1/3}$$

$$V = \frac{4}{3}\pi R^3 \propto A$$

Mass  $\propto A$ 

So density is independent of A.



- 12. An object of mass 1 kg is taken to a height from the surface of earth which is equal to three times the radius of earth. The gain in potential energy of the object will be [If,  $g=10ms^{-2}$  and radius of earth = 6400 km] (A) 48 MJ (B) 24 MJ
  - (C) 36 MJ (D) 12 MJ

Official Ans. by NTA (A)

Sol. 
$$U_{i} = \frac{-GMm}{R}$$
$$U_{f} = -\frac{GMm}{4R}$$
$$\Delta U = U_{f} - U_{i} = \frac{3GMm}{4R}$$
$$= \frac{3}{4}mgR$$
$$= \frac{3}{4} \times 1 \times 10 \times 64 \times 10^{5}$$
$$= 48 \text{ MJ}$$

13. A ball is released from a height h. If  $t_1$  and  $t_2$  be the time required to complete first half and second half of the distance respectively. Then, choose the correct relation between  $t_1$  and  $t_2$ .

(A)  $t_1 = (\sqrt{2})t_2$  (B)  $t_1 = (\sqrt{2}-1)t_2$ (C)  $t_2 = (\sqrt{2}+1)t_1$  (D)  $t_2 = (\sqrt{2}-1)t_1$ Official Ans. by NTA (D)

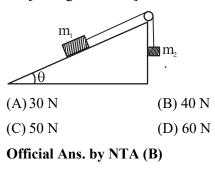
**Sol.** For first  $\frac{h}{2}$ 

$$\frac{h}{2} = \frac{1}{2}gt_1^2$$

For total height h

$$h = \frac{1}{2}g(t_1 + t_2)^2$$
$$\frac{1}{\sqrt{2}} = \frac{t_1}{t_1 + t_2}$$
$$1 + \frac{t_2}{t_1} = \sqrt{2}$$
$$\frac{t_1}{t_2} = \frac{1}{\sqrt{2} - 1}$$
$$t_2 = (\sqrt{2} - 1)t_1$$

14. Two bodies of masses  $m_1 = 5$  kg and  $m_2 = 3$  kg are connected by a light string going over a smooth light pulley on a smooth inclined plane as shown in the figure. The system is at rest. The force exerted by the inclined plane on the body of mass  $m_1$  will be :[Take g = 10 ms<sup>-2</sup>]



**Sol.** For equilibrium 
$$m_2g = m_1g \sin\theta$$

$$\sin \theta = \frac{m_2}{m_1} = \frac{3}{5}$$
$$\cos \theta = \frac{4}{5}$$

Normal force on  $m_1 = 5g \cos\theta$ 

$$=5\times10\times\frac{4}{5}=40\,\mathrm{N}$$

15. If momentum of a body is increased by 20%, then its kinetic energy increases by :

Official Ans. by NTA (C)

Sol. 
$$P' = P + \frac{20}{100}P = 1.2 P$$
  
% change in  $KE = \frac{K' - K}{K} \times 100$   
 $= \left(\frac{\frac{P'^2}{2m} - \frac{P^2}{2m}}{\frac{P^2}{2m}}\right) \times 100$   
 $= [(1.2)^2 - 1] \times 100$   
 $= 44 \%$ 

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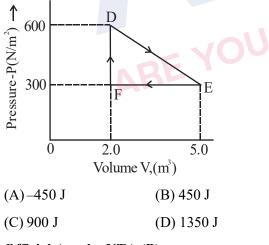
**16.** The torque of a force  $5\hat{i} + 3\hat{j} - 7\hat{k}$  about the origin **18.** The vertical c

is  $\tau$ . If the force acts on a particle whose position vector is  $2\hat{i}+2\hat{j}+\hat{k}$ , then the value of  $\tau$  will be : (A)  $11\hat{i}+19\hat{j}-4\hat{k}$  (B)  $-11\hat{i}+9\hat{j}-16\hat{k}$ (C)  $-17\hat{i}+19\hat{j}-4\hat{k}$  (D)  $17\hat{i}+9\hat{j}+16\hat{k}$ 

Official Ans. by NTA (C)

Sol. 
$$\vec{\tau} = \vec{r} \times \vec{F} = \begin{vmatrix} i & j & k \\ 2 & 2 & 1 \\ 5 & 3 & -7 \end{vmatrix}$$
  
=  $i(-14-3) - j(-14-5) + \hat{k}(6-10)$   
=  $-17\hat{i} + 19\hat{j} - 4\hat{k}$ 

17. A thermodynamic system is taken from an original state D to an intermediate state E by the linear process shown in the figure. Its volume is then reduced to the original volume from E to F by an isobaric process. The total work done by the gas from D to E to F will be



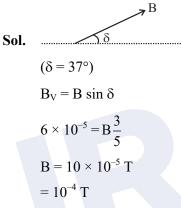
Official Ans. by NTA (B)

Sol. 
$$W_{DE} = \frac{1}{2} (600 + 300) 3 J$$
  
= 1350 J  
 $W_{EF} = -300 \times 3 = -900 J$   
 $W_{DEE} = 450 J$ 

**18.** The vertical component of the earth's magnetic field is  $6 \times 10^{-5}$  T at any place where the angle of dip is 37°. The earth's resultant magnetic field at that place will be (Given tan  $37^{\circ} = \frac{3}{4}$ )

(A) 
$$8 \times 10^{-5}$$
 T (B)  $6 \times 10^{-5}$  T  
(C)  $5 \times 10^{-4}$  T (D)  $1 \times 10^{-4}$  T

Official Ans. by NTA (D)



19. The root mean square speed of smoke particles of mass  $5 \times 10^{-17}$  kg in their Brownian motion in air at NTP is approximately. [Given  $k = 1.38 \times 10^{-23}$  JK<sup>-1</sup>] (A) 60 mm s<sup>-1</sup> (B) 12 mm s<sup>-1</sup> (C) 15 mm s<sup>-1</sup> (D) 36 mm s<sup>-1</sup>

Official Ans. by NTA (C)

Sol. 
$$V_{\rm rms} = \sqrt{\frac{3kT}{m}} = \sqrt{\frac{3 \times 1.38 \times 10^{-23} \times 293}{5 \times 10^{-17}}}$$
  
\$\approx 15 mm/s

20. Light enters from air into a given medium at an angle of 45° with interface of the air-medium surface. After refraction, the light ray is deviated through an angle of 15° from its original direction. The refractive index of the medium is :

(C) 1.414 (D)	2.732
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Official Ans. by NTA (C)



#### **SECTION-B**

1. A tube of length 50 cm is filled completely with an incompressible liquid of mass 250 g and closed at both ends. The tube is then rotated in horizontal plane about one of its ends with a uniform angular velocity  $x\sqrt{F}$  rad s<sup>-1</sup>. If F be the force exerted by the liquid at the other end then the value of x will be \_\_\_\_\_.

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#### Official Ans. by NTA (4)



Sol.

$$F = \int (dm)\omega^{2}x$$
$$= \int_{0}^{L} \left(\frac{m}{L}dx\right)\omega^{2}x$$
$$= \frac{m}{L}\omega^{2}\frac{L^{2}}{2}$$
$$= \frac{m\omega^{2}L}{2}$$
$$\omega = \sqrt{\frac{2}{mL}}\sqrt{F}$$
$$= \sqrt{\frac{2}{0.25 \times 0.5}}\sqrt{F}$$
$$= \sqrt{16}\sqrt{F}$$
$$= 4\sqrt{F}$$

2. Nearly 10% of the power of a 110 W light bulb is converted to visible radiation. The change in average intensities of visible radiation, at a distance of 1 m from the bulb to a distance of 5 m is  $a \times 10^{-2}$  W/m<sup>2</sup>. The value of 'a' will be

Official Ans. by NTA (84)

Sol. 
$$P' = 10\%$$
 of 110 W

$$= \frac{10}{100} \times 110 W$$
  
= 11 W  
$$I_1 - I_2 = \frac{P'}{4\pi r_1^2} - \frac{P'}{4\pi r_2^2}$$
  
$$= \frac{11}{4\pi} \left[ \frac{1}{1} - \frac{1}{25} \right]$$
  
$$= \frac{11}{4\pi} \times \frac{24}{25}$$
  
$$= \frac{264}{\pi} \times 10^{-2} = 84 \times 10^{-2} W / m^2$$

A metal wire of length 0.5 m and cross-sectional area  $10^{-4}$  m<sup>2</sup> has breaking stress 5 ×  $10^{8}$  Nm<sup>-2</sup>. A block of 10 kg is attached at one end of the string and is rotating in a horizontal circle. The maximum linear velocity of block will be ms<sup>-1</sup>.

Official Ans. by NTA (50)

Sol. 
$$T = \frac{mv^2}{\ell} = \frac{10 \times v^2}{0.5} = 20v^2$$
$$T_{max} = Breaking stress \times Area$$
$$= 5 \times 10^8 \times 10^{-4} = 5 \times 10^4$$
$$20V^2 = 5 \times 10^4$$
$$V = \sqrt{\frac{1}{4}10^4} = 50 \text{ m/s}$$

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- 4. The velocity of a small ball of mass 0.3g and string of length
- density 8g/cc when dropped in a container filled with glycerine becomes constant after some time. If the density of glycerine is 1.3 g/cc, then the value of viscous force acting on the ball will be

 $x \times 10^{-4}$  N, the value of x is \_\_\_\_\_. [use g = 10m/s<sup>2</sup>]

Official Ans. by NTA (25)

Sol.  $F_V + F_B = mg (v = constant)$   $F_V = mg - F_B$   $= \rho_B Vg - \rho_L Vg$   $= (\rho_B - \rho_L) Vg$   $= (8 - 1.3) \times 10^{+3} \times \frac{0.3 \times 10^{-3}}{8 \times 10^3} \times 10$   $= \frac{6.7 \times 0.3}{8} \times 10^{-2} \quad (g = 10)$  $= \frac{67 \times 3}{8} \times 10^{-4} = 25.125 \times 10^{-4}$ 

Ans. 25.125

5. A modulating signal  $2\sin(6.28 \times 10^6)$ t is added to the carrier signal  $4\sin(12.56 \times 10^9)$ t for amplitude modulation. The combined signal is passed through a non-linear square law device. The output is then passed through a band pass filter. The bandwidth of the output signal of band pass filter will be\_\_\_MHz.

Official Ans. by NTA (2)

Sol. Frequencies present in output of square law device  $2f_c$ ,  $f_c + f_m$ ,  $f_c$ ,  $f_c - f_m$ ,  $2f_m$ ,  $f_m$ After passing through band bass filte.  $f_c + f_m$ ,  $f_c$ ,  $f_c - f_m$ Band width =  $2f_m$ 

$$=\frac{2\omega_{\rm m}}{2\pi}=\frac{6.28\times10^6}{3.14}$$
$$=2 \text{ MHz}$$

The speed of a transverse wave passing through a string of length 50 cm and mass 10 g is 60 ms<sup>-1</sup>. The area of cross-section of the wire is 2.0 mm<sup>2</sup> and its Young's modulus is  $1.2 \times 10^{11}$  Nm<sup>-2</sup>. The extension of the wire over its natural length due to its tension will be  $x \times 10^{-5}$  m. The value of x is \_\_\_\_\_.

Official Ans. by NTA (15)

Sol. 
$$V_w = \sqrt{\frac{T}{\mu}}$$
  
 $60 = \sqrt{\frac{T}{10 \times 10^{-3}} \times 0.5}$   
 $T = \frac{(60)^2 \times 10^{-2}}{0.5} = 72 \text{ N}$   
 $\Delta \ell = \frac{F\ell}{AY} = \frac{72 \times 0.5}{2 \times 10^{-6} \times 1.2 \times 10^{11}}$   
 $= \frac{72 \times 5}{24} \times 10^{-5} = 15 \times 10^{-5}$   
Ans. 15

The metallic bob of simple pendulum has the relative density 5. The time period of this pendulum is 10 s. If the metallic bob is immersed in water, then the new time period becomes  $5\sqrt{x}$  s. The value of x will be

Official Ans. by NTA (5)

7.

Sol. mg' = mg - F<sub>B</sub>  

$$F_{B}$$

$$g' = \frac{mg - F_{B}}{m}$$

$$g' = \frac{mg - F_{B}}{m}$$

$$g' = \frac{\rho_{B}Vg - \rho_{w}Vg}{\rho_{B}V}$$

$$g' = \left(\frac{\rho_{B} - \rho_{w}}{\rho_{B}}\right)g \quad T = 2\pi\sqrt{\frac{\ell}{g}}$$

$$g' = \frac{5 - 1}{5} \times g$$

$$g' = \frac{4}{5}g$$

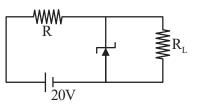
$$T' = \sqrt{\frac{g}{g'}} = \sqrt{\frac{g}{\frac{4}{5}g}} = \sqrt{\frac{5}{4}}$$

$$T' = T\sqrt{\frac{5}{4}} = \frac{10}{2}\sqrt{5}$$

$$T' = 5\sqrt{5}$$



A 8 V Zener diode along with a series resistance R 8. is connected across a 20 V supply (as shown in the figure). If the maximum Zener current is 25 mA, then the minimum value of R will be  $\Omega$ .



Official Ans. by NTA (480)

- **Sol.**  $\varepsilon IR V_z = 0$ 20 - IR - 6 = 0IR = 12 $25 \times 10^{-3} \text{ R} = 12$  $R = \frac{12}{25 \times 10^{-3}} = 480\Omega$
- 9. Two radioactive materials A and B have decay constants  $25\lambda$  and  $16\lambda$  respectively. If initially they have the same number of nuclei, then the ratio of the number of nuclei of B to that of A will be "e"

after a time  $\frac{1}{a\lambda}$ . The value of a is\_

Official Ans. by NTA (9)

Official Ans. by NTA (9)  
Sol. 
$$N = N_0 e^{-\lambda t}$$
  
 $\frac{N_B}{N_A} = \frac{e^{-\lambda_2 t}}{e^{-\lambda_1 t}} = e^{-\lambda_2 t} \cdot e^{\lambda_1 t}$   
 $e^1 = e^{(\lambda_1 - \lambda_2)t}$   
 $(\lambda_1 - \lambda_2)t = 1$   
 $t = \frac{1}{\lambda_1 - \lambda_2} = \frac{1}{25\lambda - 16\lambda} = \frac{1}{9\lambda}$ 

10. A capacitor of capacitance 500 µF is charged completely using a dc supply of 100 V. It is now connected to an inductor of inductance 50 mH to form an LC circuit. The maximum current in LC circuit will be A.

Official Ans. by NTA (10)

Energy stored in capacitor Sol.

 $=\frac{5}{2}J$ 

$$=\frac{1}{2}CV^{2}=\frac{1}{2}500\times10^{-6}\times10^{4}$$

Current will be maximum when whole energy of capacitor becomes energy of inductor.

$$\frac{1}{2}LI^{2} = \frac{5}{2}$$

$$I = \sqrt{\frac{5}{L}} = \sqrt{\frac{5}{50 \times 10^{-3}}} = 10 \text{ A}.$$



FINAL JEE-MAIN EXAMINATION - JULY, 2022 (Held On Friday 29th July, 2022) TIME: 3:00 PM to 06:00 PM **CHEMISTRY** TEST PAPER WITH SOLUTION **SECTION-A Sol.** Energy order of subshell decided by  $(n+\lambda)$  rule.  $A \Rightarrow 3d \Rightarrow n + 1 = 5$ 1. Consider the reaction  $B \Longrightarrow 4 p \Longrightarrow n + \lambda = 5$  $4HNO_3(l) + 3KCl(s) \rightarrow Cl_2(g) + NOCl(g) +$  $C \Rightarrow 4d \Rightarrow n + \ell \Rightarrow 6$  $2H_2O(g) + 3KNO_3(s)$  $D \Rightarrow 3s \Rightarrow (n+\ell) = 4$ The amount of HNO<sub>3</sub> required to produce 110.0 g  $D \le A \le B \le C$ of KNO<sub>3</sub> is :  $C(s) + O_2(g) \rightarrow CO_2(g) + 400 \text{ kJ}$ 3. (Given : Atomic masses of H, O, N and K are 1,  $C(s) + \frac{1}{2}O_2(g) \rightarrow CO(g) + 100 \text{ kJ}$ 16, 14 and 39, respectively.) (A) 32.2 g When coal of purity 60% is allowed to burn in (B) 69.4 g presence of insufficient oxygen, 60% of carbon is (C) 91.5 g (D) 162.5 g converted into 'CO' and the remaining is converted Official Ans. by NTA (C) into 'CO<sub>2</sub>'. The heat generated when 0.6 kg of coal is burnt is Sol.  $4HNO_{3}(\ell) + 3KCl(s) \rightarrow Cl_{2}(g) + NOCl(g) + 2H_{2}O(g) + 3KNO_{3}(g)$ (A) 1600 kJ (B) 3200 kJ 110 gm x gm (C) 4400 kJ (D) 6600 kJ Official Ans. by NTA (D)  $Mole = \frac{110}{101}$  $\frac{x}{63}$  $C(S) + O_2(g) \rightarrow CO_2(g) + 400 \text{ kJ}$ Sol.  $4 \rightarrow 3$ 1 g mole  $\frac{x}{63} \rightarrow \frac{3}{4} \times \frac{x}{63} = \frac{110}{101}$  $1 \rightarrow \frac{3}{4}$  $C(s) + \frac{1}{2}O_2(g) \rightarrow CO(g) + 100kJ \dots (II)$  $0.6 \times 1000$ = 600 gm $600 \times \frac{60}{100}$  (Pure Carbon)  $x = \frac{110 \times 63 \times 4}{101 \times 3} = 91.5 \,\mathrm{gm}$  $=360 \text{gm} = \frac{360}{12} = 30 \text{mole}$  (Pure Carbon) Given below are the quantum numbers for 4 2. electrons. Carbon converted into  $CO_2 = \left(30 - 30 \times \frac{60}{100}\right)$ A. n = 3, l = 2,  $m_1 = 1$ ,  $m_s = +1/2$ = 12 moleB. n = 4, l = 1,  $m_1 = 0$ ,  $m_s = +1/2$ and carbon converted in CO =  $30 \times \frac{60}{100} = 18$  mole C. n = 4, l = 2,  $m_1 = -2$ ,  $m_s = -1/2$ D. n = 3, l = 1,  $m_1 = -1$ ,  $m_s = +1/2$ Energy generated during II equation The correct order of increasing energy is :  $= 18 \times 100$ = 1800 kJ(A) D < B < A < C(B) D < A < B < CEnergy generated during I<sup>st</sup> reaction. (C) B < D < A < C(D) B < D < C < A $= 12 \times 400$ Official Ans. by NTA (B) =4800Total = 1800 + 4800 = 6600 kJ



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4. 200 mL of 0.01 M HCl is mixed with 400 mL of 0.01M H<sub>2</sub>SO<sub>4</sub>. The pH of the mixture is \_\_\_\_\_.
(A) 1.14 (B) 1.78

(C) 2.34 (D) 3.02

Official Ans. by NTA (B)

Sol.  $HCl + H_2SO_4$ 

$$[H^+] = \frac{(0.01 \times 200) + (0.01 \times 2 \times 400)}{600}$$
$$= \frac{2+8}{600} = \frac{10}{600} = \frac{1}{60}$$
$$pH = -\log\left[\frac{1}{60}\right]$$
$$= 1.78$$

5. Given below are the critical temperatures of some of the gases :

Gas	Critical temperature (K)		
He	5.2		
CH <sub>4</sub>	190		
$CO_2$	304.2		
NH <sub>3</sub>	405.5		

The gas showing least adsorption on a definite amount of charcoal is :

Official Ans. by N	TA (A)
(C) CO <sub>2</sub>	(D) NH <sub>3</sub>
(A) He	(B) CH <sub>4</sub>

- **Sol.** More the critical temp. of gas greater is the ease of liquefaction hence greater is the adsorption.
- **6.** In liquation process used for tin (Sn), the metal :
  - (A) is reacted with acid
  - (B) is dissolved in water
  - (C) is brought to molten form which is made to flow on a slope
  - (D) is fused with NaOH.

Official Ans. by NTA (C)

**Sol.** Liquation process is used for metal having low melting point such as tin in which they are heated and brought to molten state and made to flow down the slope while impurities with higher melting point left on the top.

- Given below are two statements.
  Statement I : Stannane is an example of a molecular hydride.
  Statement II : Stannane is a planar molecule.
  In the light of the above statement, choose the most appropriate answer from the options given below :
  (A) Both Statement I and Statement II are true.
  (B) Both Statement I and Statement II are false.
  (C) Statement I is true but Statement II is false.
  (D) Statement I is false but Statement II is true.
  Official Ans. by NTA (C)
- **Sol.**  $SnH_4$  is non planar molecular hydride

7.

<sup>II</sup> Tetrahedral shape, sp<sup>3</sup> hybridisation

8. Portland cement contains 'X' to enhance the setting time. What is 'X'?

(A) CaSO<sub>4</sub>.  $\frac{1}{2}$  H<sub>2</sub>O (B) CaSO<sub>4</sub>.2H<sub>2</sub>O (C) CaSO<sub>4</sub> (D) CaCO<sub>3</sub> Official Ans. by NTA (B)

- **Sol.** Gypsum (CaSO<sub>4</sub>.2H<sub>2</sub>O) is used to enhance setting time in portland cement.
- 9. When borax is heated with CoO on a platinum loop, blue coloured bead formed is largely due to :
  (A) B<sub>2</sub>O<sub>3</sub>
  (B) Co(BO<sub>2</sub>)<sub>2</sub>
  (C) CoB<sub>4</sub>O<sub>7</sub>
  (D) Co[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]
  Official Ans. by NTA (B)
- Sol.  $Na_2B_4O_7 10H_2O \xrightarrow{\Delta} Na_2B_4O_7 + 10H_2O$   $Na_2B_4O_7 \xrightarrow{\Delta} 2NaBO_2(\text{sodium meta borate}) + B_2O_3$   $B_2O_3 + CoO \rightarrow Co(BO_2)_2(\text{cobalt (II) meta borate})$ Blue Bead
- 10. Which of the following 3d-metal ion will give the lowest enthalpy of hydration  $(\Delta_{hyd}H)$  when dissolved in water ?

(A) 
$$Cr^{2+}$$
 (B)  $Mn^{2+}$   
(C)  $Fe^{2+}$  (D)  $Co^{2+}$   
Official Ans. by NTA (B)

Sol.

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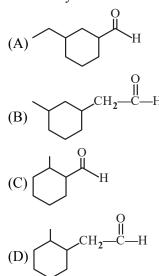
11. Octahedral complexes of copper (II) undergo structural distortion (Jahn-Teller). Which one of the given copper (II) complexes will show the maximum structural distortion ?

(en-ethylenediamine; H<sub>2</sub>N-CH<sub>2</sub>-CH<sub>2</sub>-NH<sub>2</sub>)
(A) [Cu(H<sub>2</sub>O)<sub>6</sub>]SO<sub>4</sub>
(B) [Cu(en)(H<sub>2</sub>O)<sub>4</sub>]SO<sub>4</sub>
(C) cis-[Cu(en)<sub>2</sub>Cl<sub>2</sub>]
(D) trans-[Cu(en)<sub>2</sub>Cl<sub>2</sub>]

Official Ans. by NTA (A)

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- **Sol.** There is unsymmetric filling of  $e_g$  subset of  $Cu^{+2}$  ion, while there is symmetrical distribution in  $t_{2g}$  set, if the complex has same ligand there will be equal repulsion which leads to symmetrical bond length along  $t_{2g}$ , but due to uneven filling of electron in  $e_g$  subset, either octahedral will be elongated or compressed.
- 12. Dinitrogen is a robust compound, but reacts at high altitude to form oxides. The oxide of nitrogen that can damage plant leaves and retard photosynthesis is :
  - (A) NO (B)  $NO_3^-$ (C)  $NO_2$  (D)  $NO_2^-$
  - Official Ans. by NTA (C)
- Sol.  $N_2(g) + O_2(g) \rightarrow 2NO(g)$   $2NO(g) + O_2(g) \rightarrow 2NO_2(g)$  $NO_2$  damage plant leaves
- **13.** Correct structure of γ-methylcyclohexane carbaldehyde is :



Official Ans. by NTA (A)

γ-methyl cyclohexane carbaldehyde

14. Compound 'A' undergoes following sequence of reactions to give compound 'B'. The correct structure and chirality of compound 'B' is: [where Et is -C<sub>2</sub>H<sub>5</sub>]

$$(A) \xrightarrow{(i)Mg,Et_2O} B$$

$$(A) \xrightarrow{(i)Mg,Et_2O} B$$

$$(A) \xrightarrow{(i)D_2O} B$$

$$(A) \xrightarrow{(i)D_2O} A$$

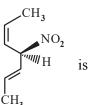
$$(A) \xrightarrow{(i)D_2O} B$$

$$(B) \xrightarrow{(i)D_2O} A$$

Official Ans. by NTA (C)

Sol. 
$$\searrow$$
  $(i) Mg, \epsilon t_2 o$   
Br  $(ii) D_2 O \Rightarrow B$ 

Statement I : The compound



optically active.

Statement II : 
$$O_2N$$
 is mirror image of  $CH_3$ 

OTI

above compound A.

In the light of the above statement, choose the **most appropriate** answer from the options given below.

(A) Both Statement I and Statement II are correct

(B) Both Statement I and Statement II are incorrect.

(C) Statement I is correct but Statement II is incorrect.

(D) Statement I is incorrect but Statement II is correct.

Official Ans. by NTA (C)



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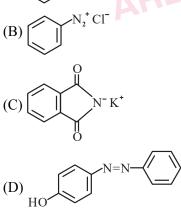
Having same configuration.

- When enthanol is heated with conc. H<sub>2</sub>SO<sub>4</sub>, a gas is produced. The compound formed, when this gas is treated with cold dilute aqueous solution of Baeyer's reagent, is :
  - (A) Formaldehyde(B) Formic acid(C) Glycol(D) Ethanoic acid

Official Ans. by NTA (C)

Sol. 
$$CH_3-CH_2-OH \xrightarrow{\text{conc. } H_2SO_4}{\Delta} CH_2=CH_2$$
  
 $Bayer's Reagent CH_2 - CH_2 \ | DH OH OH OH$ 

17. The Hinsberg reagent is :



Official Ans. by NTA (A)

Sol.

B.S.C (Benzene sulphonyl chloride) is known's Hinsberg Reagent

- **18.** Which of the following is **NOT** a natural polymer?
  - (A) Protein
  - (B) Starch
  - (C) Rubber
  - (D) Rayon
  - Official Ans. by NTA (D)
- Sol. Rayon is semisynthetic polymer.
- 19. Given below are two statements. One is labelled as
  Assertion A and the other is labelled as Reason R.
  Assertion A : Amylose is insoluble in water.

**Reason R :** Amylose is a long linear molecule with more than 200 glucose units.

In the light of the above statements, choose the correct answer from the options given below.

(A) Both A and R are correct and R is the correct explanation of A.

(B) Both A and R are correct and R is NOT the correct explanation of A.

(C) A is correct but **R** is not correct.

(D) **A** is not correct but **R** is correct.

Official Ans. by NTA (D)

**Sol.** Amylose is water soluble.

20. A compound 'X' is a weak acid and it exhibits colour change at pH close to the equivalence point during neutralization of NaOH with CH<sub>3</sub>COOH. Compound 'X' exists in ionized form in basic medium. The compound 'X' is :

(A) methyl orange
(B) methyl red
(C) phenolphthalein
(D) erichrome Black T
Official Ans. by NTA (C)

Sol. Phenolphthalein is weak acid give colour in basic medium.

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### **SECTION-B**

'x' g of molecular oxygen (O<sub>2</sub>) is mixed with 200 g of neon (Ne). The total pressure of the non-reactive mixture of O<sub>2</sub> and Ne in the cylinder is 25 bar. The partial pressure of Ne is 20 bar at the same temperature and volume. The value of 'x' is \_\_\_\_\_.

[Given: Molar mass of  $O_2 = 32 \text{ g mol}^{-1}$ .

Molar mass of  $Ne = 20 \text{ g mol}^{-1}$ ]

Official Ans. by NTA (80)

Sol. 
$$O_2 + Ne$$

Xgm 200gm

 $P_{total} = 25 \text{ bar}; P_{Ne} = 20$  $P_{O_2} + P_{Ne} = 25$ 

 $P_{O_2} = 25 - 20 = 5 \text{ bar}$ 

$$5 = \frac{\frac{x}{32}}{\frac{x}{32} + \frac{200}{20}} \times 25$$
  

$$\frac{1}{5} = \frac{\frac{x}{32}}{\frac{x}{32} + 10}$$
  

$$\frac{1}{5} = \frac{x \times 32}{32(x + 320)}$$
  

$$5x = x + 320$$
  

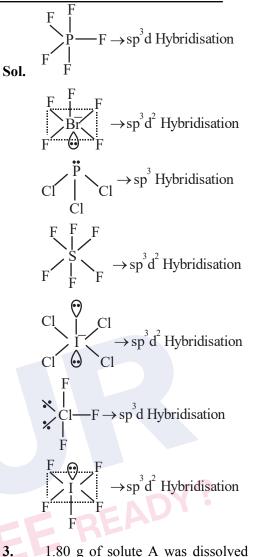
$$4x = 320$$
  

$$x = \frac{320}{4} = 80 \text{ gm}$$

2. Consider,  $PF_5$ ,  $BrF_5$ ,  $PCl_3$ ,  $SF_6$ ,  $[ICl_4]^-$ ,  $ClF_3$  and  $IF_5$ .

Amongst the above molecule(s)/ion(s), the number of molecule(s)/ion(s) having sp<sup>3</sup>d<sup>2</sup> hybridisation is\_\_\_\_.

Official Ans. by NTA (4)



1.80 g of solute A was dissolved in 62.5 cm<sup>3</sup> of ethanol and freezing point of the solution was found to be 155.1 K. The molar mass of solute A is  $\_g \text{ mol}^{-1}$ .

[Given: Freezing point of ethanol is 156.0 K. Density of ethanol is  $0.80 \text{ g cm}^{-3}$ .

Freezing point depression constant of ethanol is 2.00 K kg mol<sup>-1</sup>]

Official Ans. by NTA (80)

Sol. Mass of C<sub>2</sub>H<sub>5</sub>OH =  $62.5 \times 0.8 = 50$  g  $\Delta T_f = K_f \times m$ 

$$0.9 = 2 \times \frac{1.8 \times 1000}{M_{w} \times 50}$$
$$M_{w} = \frac{2 \times 1.8 \times 1000}{0.9 \times 50} = 80$$



4. For a cell, Cu(s)  $|Cu^{2+}(0.001M)| |Ag^{+}(0.01M)| |Ag(s)$ the cell potential is found to be 0.43 V at 298 K. The magnitude of standard electrode potential for  $Cu^{2+}/Cu$  is  $\underline{\phantom{aaaa}} \times 10^{-2}$  V.

$$\left[\text{Given}: E_{Ag^+/Ag}^{\Theta} = 0.80 \text{ V and } \frac{2.303 \text{ RT}}{\text{F}} = 0.06 \text{ V}\right]$$

Official Ans. by NTA (34)

Sol. At anode

Cu → Cu<sup>2+</sup> + 2e<sup>-</sup> At cathode 2Ag<sup>+</sup> + 2e<sup>-</sup> → 2Ag Cell reaction → Cu + 2Ag<sup>+</sup> → Cu<sup>2+</sup> + 2Ag  $E_{cell} = E_{cell}^{0} - \frac{0.06}{2} \log \frac{[Cu^{2+}]}{[Ag^{+}]^{2}}$ 0.43 =  $E_{cell}^{0} - \frac{0.06}{2} \log \frac{(0.001)}{(0.01)^{2}}$   $E_{cell}^{0} = 0.46$   $E_{cell}^{0} = E_{Ag^{+}/Ag}^{0} - E_{Cu^{2+}/Cu}^{0}$ 0.46 = 0.80 -  $E_{Cu^{2+}/Cu}^{0}$   $E_{Cu^{2+}/Cu}^{0} = 0.34$  volt  $E_{Cu^{2+}/Cu}^{0} = 34 \times 10^{-2}$ 

5. Assuming 1µg of trace radioactive element X with a half life of 30 years is absorbed by a growing tree. The amount of X remaining in the tree after 100 years is  $\_\times 10^{-1}$ µg.

[Given :  $\ln 10 = 2.303$ ;  $\log 2 = 0.30$ ]

Official Ans. by NTA (1)

Sol. 
$$t = \frac{1}{\lambda} \ell n \left( \frac{a}{a - x} \right)$$
$$100 = \frac{30}{\ell n 2} \ell n \left( \frac{1}{w} \right)$$
$$\frac{1}{w} = 10$$
$$W = 0.1 \times \mu g$$
Ans.  $1 \times 10^{-1} \mu g$ 

6. Sum of oxidation state (magnitude) and coordination number of cobalt in Na[Co(bpy)Cl<sub>4</sub>] is\_\_.

(Given bpy = 
$$N$$
 N)

Official Ans. by NTA (9)

- Sol. Coordination no. = 6 Oxidation state = 3 6+3=9
- Consider the following sulphure based oxoacids.
   H<sub>2</sub>SO<sub>3</sub>, H<sub>2</sub>SO<sub>4</sub>, H<sub>2</sub>S<sub>2</sub>O<sub>8</sub> and H<sub>2</sub>S<sub>2</sub>O<sub>7</sub>.
   Amongst these oxoacids the number of those with

Amongst these oxoacids, the number of those with peroxo(O-O) bond is\_\_\_\_\_.

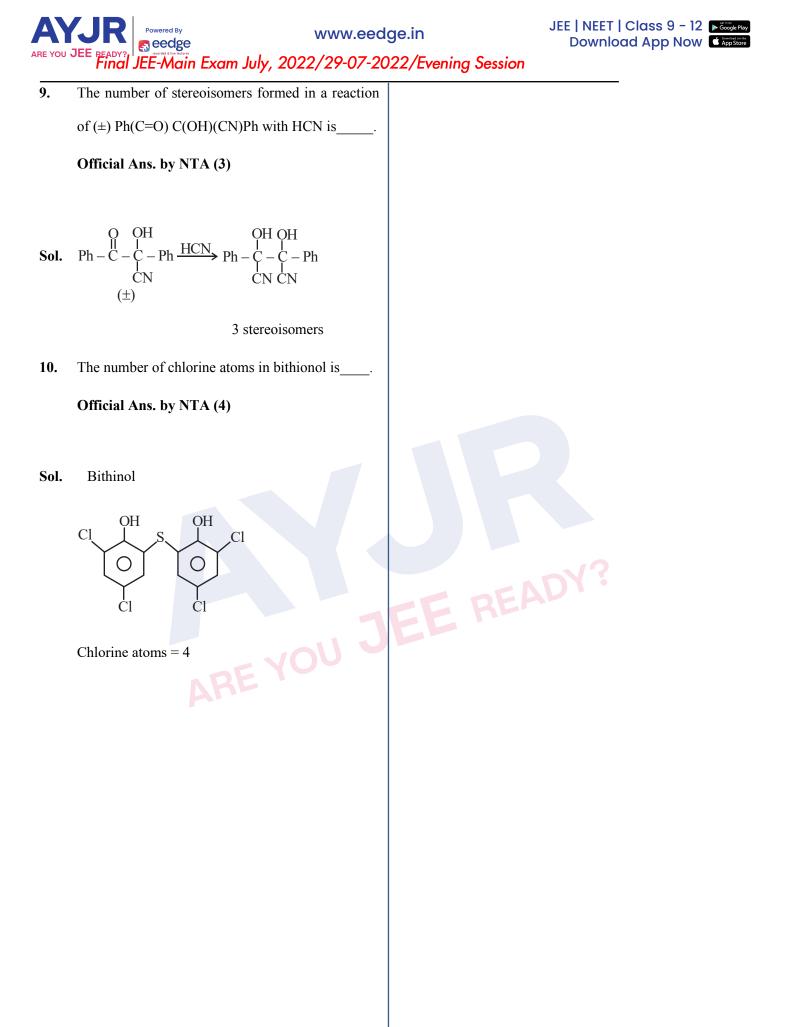
Official Ans. by NTA (1)

Sol. 
$$H-O-S-O-H (H_2SO_3)$$
  
 $H-O-S-O-H (H_2SO_4)$   
 $H-O-S-O-O-S-OH (H_2S_2O_8)$   
 $HO-S-O-O-S-OH (H_2S_2O_8)$   
 $H-O-S-O-S-OH (H_2S_2O_7)$   
 $H=O-S-O-S-OH (H_2S_2O_7)$ 

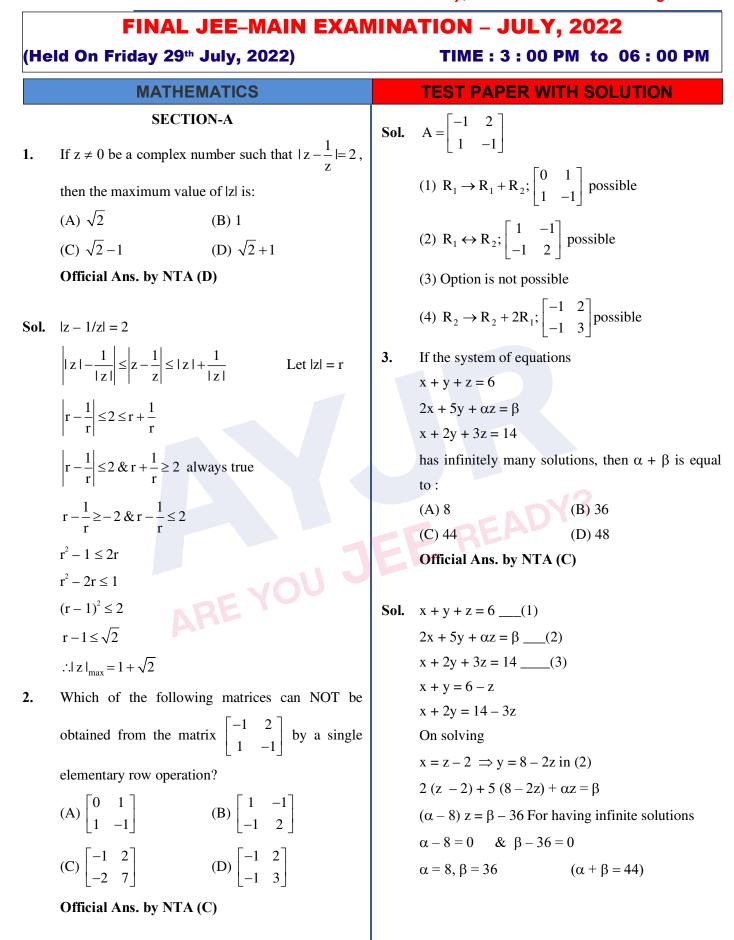
8. A 1.84 mg sample of polyhydric alcoholic compound 'X' of molar mass 92.0 g/mol gave 1.344 mL of H<sub>2</sub> gas at STP. The number of alcoholic hydrogens present in compound 'X' is\_\_\_\_.

Official Ans. by NTA (3)

Sol. 
$$R(OH)_x \rightarrow H_2$$
  
PoAC on H –  
 $x\left(\frac{1.84 \times 10^{-3}}{92}\right) = \frac{1.344}{22.4} \times 2$   
 $x = \frac{1.344 \times 2 \times 92 \times 1000}{1.84 \times 22400} = 6$   
 $x = 6$ 









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4. Let the function

$$f(x) = \begin{cases} \frac{\log_{e} (1+5x) - \log_{e} (1+\alpha x)}{x} ; \text{if } x \neq 0\\ 10 ; \text{if } x = 0 \end{cases}$$

be continuous at x = 0.

The  $\alpha$  is equal to :

### Official Ans. by NTA (D)

Sol. 
$$f(x) = \begin{cases} \frac{\ln(1+5x) - \ln(1+\alpha x)}{x} & ; x \neq 0\\ 10 & ; x = 0 \end{cases}$$
$$\lim_{x \to 0} \frac{\ln(1+5x) - \ln(1+\alpha x)}{x} = 10$$

Using expension

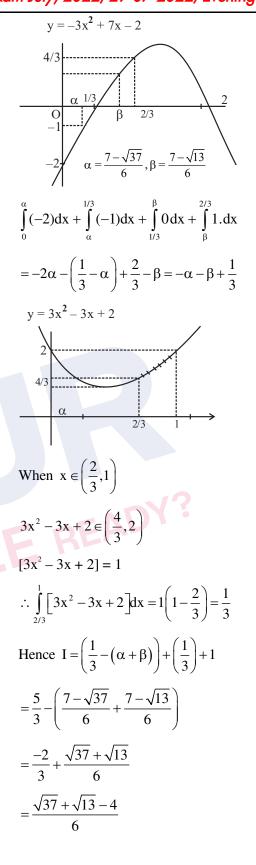
$$\lim_{x \to 0} \frac{(5x + \dots) - (\alpha x + \dots)}{x} = 10$$
  
$$5 - \alpha = 10 \Rightarrow \alpha = -5$$

5. If [t] denotes the greatest integer  $\leq$  t, then the value

of 
$$\int_{0}^{1} \left[ 2x - |3x^{2} - 5x + 2| + 1 \right] dx$$
 is:  
(A)  $\frac{\sqrt{37} + \sqrt{13} - 4}{6}$  (B)  $\frac{\sqrt{37} - \sqrt{13} - 4}{6}$   
(C)  $\frac{-\sqrt{37} - \sqrt{13} + 4}{6}$  (D)  $\frac{-\sqrt{37} + \sqrt{13} + 4}{6}$ 

Official Ans. by NTA (A)

Sol. 
$$I = \int_{0}^{1} \left[ 2x - |3x^{2} - 3x - 2x + 2| + 1 \right] dx$$
$$I = \int_{0}^{1} \left[ 2x - |(3x - 2)(x - 1)| \right] dx + \int_{0}^{1} 1 dx$$
$$I = \int_{0}^{2/3} \left[ \left( 2x - (3x^{2} - 5x + 2)) \right] dx + \int_{2/3}^{1} \left( 2x + (3x^{2} - 5x + 2)) \right) dx + 1$$
$$I = \int_{0}^{2/3} \left[ -3x^{2} + 7x - 2 \right] dx + \int_{2/3}^{1} \left( 3x^{2} - 3x + 2 \right) dx + 1$$



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Let  $\{a_n\}_{n=0}^{\infty}$  be a sequence such that  $a_0 = a_1 = 0$  and 6.  $a_{n+2} = 3a_{n+1} - 2a_n + 1, \forall n \ge 0.$ Then  $a_{25} a_{23} - 2 a_{25} a_{22} - 2 a_{23} a_{24} + 4 a_{22} a_{24}$  is equal to: (A) 483 (B) 528 (C) 575 (D) 624 Official Ans. by NTA (B) **Sol.**  $a_0 = 0, a_1 = 0$  $a_{n+2} = 3 a_{n+1} - 2 a_{n+1} : n \ge 0$  $a_{n+2} - a_{n+1} = 2 (a_{n+1} - a_n) + 1$ n = 0 $a_2 - a_1 = 2(a_1 - a_0) + 1$  $a_3 - a_2 = 2(a_2 - a_1) + 1$ n = 1  $a_4 - a_3 = 2 (a_3 - a_2) + 1$ n = 2  $a_{n+2} - a_{n+1} = 2(a_{n+1} - a_n) + 1$ n = n $(a_{n+2} - a_1) - 2 (a_{n+1} - a_0) - (n+1) = 0$  $a_{n+2} = 2a_{n+1} + (n+1)$  $n \rightarrow n - 2$  $a_n - 2a_{n-1} = n - 1$ Now  $a_{25}a_{23} - 2a_{25}a_{22} - 2a_{23}a_{24} + 4a_{22}a_{24}$  $= (a_{25}-2a_{24}) (a_{23}-2a_{22}) = (24) (22) = 528$  $\sum_{r=1}^{20} (r^2 + 1)(r!)$  is equal to: 7. (B) 22! - 2 (21! (A) 22! – 21! (C) 21! – 2 (20!) (D) 21! – 20! Official Ans. by NTA (B) 20

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Sol. 
$$\sum_{x=1}^{20} (r^{2} + 1)r!$$
$$\sum_{x=1}^{20} ((r + 1)^{2} - 2r)r!$$
$$\sum_{x=1}^{20} ((r + 1)(r + 1)! - r.r!) - \sum_{r=1}^{20} r.r!$$
$$\sum_{x=1}^{20} ((r + 1)(r + 1)! - r.r!) - \sum_{r=1}^{20} ((r + 1)! - r!)$$
$$= (21.|21 - 1) - (|21 - 1)$$
$$= 20.21! = 22! - 2.21!$$

8. For 
$$I(x) = \int \frac{\sec^2 x - 2022}{\sin^{2022} x} dx$$
, if  $I\left(\frac{\pi}{4}\right) = 2^{1011}$ , then  
(A)  $3^{1010}I\left(\frac{\pi}{3}\right) - I\left(\frac{\pi}{6}\right) = 0$   
(B)  $3^{1010}I\left(\frac{\pi}{6}\right) - I\left(\frac{\pi}{3}\right) = 0$   
(C)  $3^{1011}I\left(\frac{\pi}{6}\right) - I\left(\frac{\pi}{3}\right) = 0$   
Official Ans. by NTA (A)  
Sol.  $I(x) = \int \sec^2 x . \sin^{-2022} x dx - 2022 \int \sin^{-2022} x dx$   
 $I = \tan x. (\sin x)^{-2022} + \int (2022) \tan x. (\sin x)^{-2023} \cos x dx$   
 $-2022 \int (\sin x)^{-2022} dx$   
 $I(x) = (\tan x) (\sin x)^{-2022} + C$   
At  $X = \pi/4$ ,  $2^{1011} = \left(\frac{1}{\sqrt{2}}\right)^{-2022} + C \therefore C = 0$   
Hence  $I(x) = \frac{\tan x}{(\sin x)^{2022}}$   
 $I(\pi/6) = \frac{\sqrt{3}}{(\sqrt{3}\frac{1}{2})^{2022}} = \frac{2^{2022}}{\sqrt{3}}$   
 $I(\pi/3) = \frac{\sqrt{3}}{(\sqrt{3}\frac{1}{2})^{2022}} = \frac{2^{2022}}{\sqrt{3}}$   
 $I(\pi/3) = I(\pi/6)$   
9. If the solution curve of the differential equation  
 $\frac{dy}{dx} = \frac{x + y - 2}{x - y}$  passes through the point (2,1) and  
 $(k + 1, 2), k > 0$ , then  
(A)  $2 \tan^{-1}\left(\frac{1}{k}\right) = \log_e(k^2 + 1)$   
(C)  $2 \tan^{-1}\left(\frac{1}{k}\right) = \log_e\left(\frac{k^2 + 1}{k^2}\right)$ 

Official Ans. by NTA (A)

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ol. 
$$\frac{dy}{dx} = \frac{x + y - 2}{x - y} = \frac{(x - 1) + (y - 1)}{(x - 1) - (y - 1)}$$

$$x - 1 = X, y - 1 = Y$$

$$\frac{dY}{dX} = \frac{X + Y}{X - Y}$$

$$Y = VX \qquad \frac{dY}{dX} = V + X \frac{dV}{dX}$$

$$V + X \frac{dV}{dX} = \frac{1 + V}{1 - V} \qquad X \frac{dV}{dX} = \frac{V^2 + 1}{1 - V}$$

$$\int \frac{1 - V}{1 + V^2} dV = \int \frac{dX}{X}$$

$$\int \frac{dV}{1 + V^2} - \frac{1}{2} \int \frac{2V dV}{1 + V^2} = \int \frac{dX}{X}$$

$$\tan^{-1} V - \frac{1}{2} \ln (1 + V^2) = \ln X + c$$

$$\tan^{-1} \left(\frac{Y}{X}\right) - \frac{1}{2} \ln \left(1 + \frac{Y^2}{X^2}\right) = \ln(X) + c$$

$$\tan^{-1} \left(\frac{y - 1}{x - 1}\right) - \frac{1}{2} \ln \left(1 + \frac{(y - 1)^2}{(x - 1)^2}\right) = \ln(x - 1) + Passes through (2, 1)$$

$$0 - \frac{1}{2} \ln 1 = \ln 1 + c \therefore c = 0$$
Passes through (k + 1, 2)  

$$\therefore \tan^{-1} \left(\frac{1}{k}\right) - \frac{1}{2} \ln \left(1 + \frac{1}{k^2}\right) = \ln k$$

 $2\tan^{-1}\left(\frac{1}{k}\right) = \ln(1+k^2)$ 

10. Let y = y (x) be the solution curve of the differential equation  $\frac{dy}{dx} + \left(\frac{2x^2 + 11x + 13}{x^3 + 6x^2 + 11x + 6}\right)$  $y = \frac{(x+3)}{x+1}, x > -1$ , which passes through the point (0,1). Then y (1) is equal to: (A)  $\frac{1}{2}$  (B)  $\frac{3}{2}$  (C)  $\frac{5}{2}$  (D)  $\frac{7}{2}$ 

Official Ans. by NTA (B)

Sol. 
$$\frac{dy}{dx} + \left(\frac{2x^2 + 11x + 13}{x^3 + 6x^2 + 11x + 6}\right)y = \frac{x + 3}{x + 1}$$
$$\int p(x)dx \qquad I.F. = e^{\int p(x)dx}$$
$$\int p(x)dx = \int \frac{(2x^2 + 11x + 13)dx}{(x + 1)(x + 2)(x + 3)}$$
Using partial fraction
$$\frac{2x^2 + 11x + 13}{(x + 1)(x + 2)(x + 3)} = \frac{A}{x + 1} + \frac{B}{x + 2} + \frac{C}{x + 3}$$
$$A = \frac{4}{2} = 2$$
$$B = 1$$
$$C = -1$$
$$\because \int p(x)dx = A \ln(x + 1) + B \ln(x + 2) + c \ln(x + 3)$$
$$= \ln\left(\frac{(x + 1)^2(x + 2)}{x + 3}\right)$$
$$I.F. = e^{\int p(x)dx} = \frac{(x + 1)^2(x + 2)}{(x + 3)}$$
Solution v(IF) =  $\int Q_{x}(IF)dx$ 

$$y\left(\frac{(x+1)^{2}(x+2)}{x+3}\right) = \int \left(\frac{x+3}{x+1}\right) \frac{(x+1)^{2}(x+2)}{(x+3)} dx$$
$$y\left(\frac{(x+1)^{2}(x+2)}{x+3}\right) = \frac{x^{3}}{3} + \frac{3x^{2}}{2} + 2x + c$$

Passes through (0, 1)  $C = \frac{2}{3}$ Now put x = 1  $\Rightarrow y(1) = \frac{3}{2}$ 

11. Let  $m_1$ ,  $m_2$  be the slopes of two adjacent sides of a square of side a such that  $a^2 + 11a + 3(m_2^2 + m_2^2) = 220$ . If one vertex of the square is  $(10(\cos\alpha - \sin\alpha), 10 (\sin\alpha + \cos\alpha))$ , where  $\alpha \in \left(0, \frac{\pi}{2}\right)$  and the equation of one diagonal is  $(\cos\alpha - \sin\alpha) + (\sin\alpha + \cos\alpha) = 10$ , then 72  $(\sin^4\alpha + \cos^4\alpha) + a^2 - 3a + 13$  is equal to: (A) 119 (B) 128

(C) 145 (D) 155

Official Ans. by NTA (B)

С

set

**Sol.**  $m_1m_2 = -1$ 

$$a^{2} + 11a + 3\left(m_{1}^{2} + \frac{1}{m_{1}^{2}}\right) = 220$$
  
 $m_{2}$   
A  
B  
B

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Eq. of AC

 $AC = (\cos\alpha - \sin\alpha) + (\sin\alpha + \cos\alpha) y = 10$  $BD = (\sin\alpha - \cos\alpha) x + (\sin\alpha - \cos\alpha) y = 0$ 

 $(10 (\cos \alpha - \sin \alpha), 10 (\sin \alpha - \cos \alpha))$ 

Slope of AC =  $\left(\frac{\sin\alpha - \cos\alpha}{\sin\alpha + \cos\alpha}\right) = \tan\theta = M$ 

Eq. of line making an angle  $\pi_4$  with AC

 $m_1, m_2 = \frac{m \pm \tan \frac{\pi}{4}}{1 \pm m \tan \frac{\pi}{4}}$  $= \frac{m+1}{1-m} \text{ or } \frac{m-1}{1+m}$  $\frac{\frac{\sin\alpha - \cos\alpha}{\sin\alpha + \cos\alpha} + 1}{1 - \left(\frac{\sin\alpha - \cos\alpha}{\sin\alpha + \cos\alpha}\right)}$  $\sin\alpha - \cos\alpha$  $\frac{\sin \alpha + \cos \alpha}{1 + \frac{\sin \alpha - \cos \alpha}{\sin \alpha + \cos \alpha}}$  $m_1, m_2 = \tan \alpha, \cot \alpha$ mid point of AC & BD = M (5( $\cos\alpha$ -sin $\alpha$ ), 5( $\cos\alpha$ +sin $\alpha$ )) B  $(10(\cos\alpha - \sin\alpha), 10(\cos\alpha + \sin\alpha))$  $\mathbf{a} = \mathbf{A}\mathbf{B} = \sqrt{2} \mathbf{B}\mathbf{M} = \sqrt{2} \left( 5\sqrt{2} \right) = 10$ a = 10  $\therefore a^2 + 11a + 3\left(m_1^2 + \frac{1}{m_1 2}\right) = 220$  $100 + 110 + 3 (\tan^2 \alpha + \cot^2 \alpha) = 220$ Hence  $\tan^2 \alpha = 3$ ,  $\tan^2 \alpha = \frac{1}{3} \Rightarrow \alpha = \frac{\pi}{3} \text{ or } \frac{\pi}{6}$ Now 72  $(\sin^4 \alpha + \cos^4 \alpha) + a^2 - 3a + 13$  $=72\left(\frac{9}{16}+\frac{1}{16}\right)+100-30+13$  $=72\left(\frac{5}{8}\right)+83=45+83=128$ 

12. The number of elements in the  $S = \left\{ x \in \mathbb{R} : 2\cos\left(\frac{x^2 + x}{6}\right) = 4^x + 4^{-x} \right\} \text{ is:}$ (A) 1 (B) 3 (C) 0 (D) infinite

Official Ans. by NTA (A)

**Sol.** 
$$2\cos\left(\frac{x^2 + x}{6}\right) = 4^x + 4^{-x}$$
  
L.H.S  $\leq 2$ . & R.H.S.  $\geq 2$ 

Hence L.H.S = 2 & R.H.S = 2

$$2\cos\left(\frac{x^2 + x}{6}\right) = 2 \quad 4^x + 4^{-x} = 2$$

Check x = 0 Possible hence only one solution.

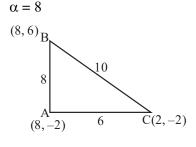
13. Let A ( $\alpha$ , -2), B ( $\alpha$ , 6) and C $\left(\frac{\alpha}{4}, -2\right)$  be vertices of a  $\triangle$ ABC. If  $\left(5, \frac{\alpha}{4}\right)$  is the circumcentre of  $\triangle$ ABC, then which of the following is NOT correct about  $\triangle$ ABC: (A) ares is 24 (B) perimeter is 25 (C) circumradius is 5 (D) inradius is 2 **Official Ans. by NTA (B)** 

**Sol.** A 
$$(\alpha, -2)$$
 : B  $(\alpha, 6)$  : C $\left(\frac{\alpha}{4}, -2\right)$ 

since AC is perpendicular to AB. So,  $\triangle$ ABC is right angled at A.

Circumcentre = mid point of BC. =  $\left(\frac{5\alpha}{8}, 2\right)$ 

$$\therefore \frac{5\alpha}{8} = 5 \& \frac{\alpha}{4} = 2$$





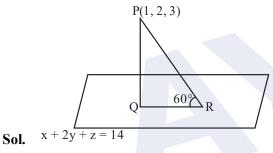
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Area = 
$$\frac{1}{2}$$
(6)(8) = 24  
Perimeter = 24  
Circumradius = 5  
Inradius =  $\frac{\Delta}{s} = \frac{24}{12} = 2$ 

Let Q be the foot of perpendicular drawn from the 14. point P (1, 2, 3) to the plane x + 2y + z = 14. If R is a point on the plane such that  $\angle PRQ = 60^\circ$ , then the area of  $\triangle PQR$  is equal to:

(A) 
$$\frac{\sqrt{3}}{2}$$
 (B)  $\sqrt{3}$   
(C)  $2\sqrt{3}$  (D) 3

Official Ans. by NTA (B)



Length of perpendicular

$$PQ = \left| \frac{1+4+3-14}{\sqrt{6}} \right| = \sqrt{6}$$

 $QR = (PQ) \cot 60^\circ = \sqrt{2}$ 

$$\therefore \text{ Area of } \Delta PQR = \frac{1}{2}(PQ)(QR) = \sqrt{3}$$

OU

If (2, 3, 9), (5, 2, 1),  $(1, \lambda, 8)$  and  $(\lambda, 2, 3)$  are 15. coplanar, then the product of all possible values of  $\lambda$  is:

(A) 
$$\frac{21}{2}$$
 (B)  $\frac{59}{8}$   
(C)  $\frac{57}{8}$  (D)  $\frac{95}{8}$ 

Official Ans. by NTA (D)

Sol. A(2, 3, 9); B(5, 2, 1); C(1, 
$$\lambda$$
, 8); D( $\lambda$ , 2, 3)  

$$\begin{bmatrix} \overline{AB} & \overline{AC} & \overline{AD} \end{bmatrix} = 0$$

$$\begin{vmatrix} 3 & -1 & -8 \\ -1 & \lambda - 3 & -1 \\ \lambda - 2 & -1 & -6 \end{vmatrix} = 0$$

$$\Rightarrow \begin{bmatrix} -6(\lambda - 3) & -1 \end{bmatrix} - 8(1 - (\lambda - 3) (\lambda - 2)) + (6 + (\lambda - 2)) = 0$$

$$3(-6 \lambda + 17) - 8(-\lambda^{2} + 5 \lambda - 5) + (\lambda + 4) = 8$$

$$8 \lambda^{2} - 57 \lambda + 95 = 0$$

$$\lambda_{1} \lambda_{2} = \frac{95}{8}$$

16. Bag I contains 3 red, 4 black and 3 white balls and Bag II contains 2 red, 5 black and 2 white balls. One ball is transferred from Bag I to Bag II and then a ball is draw from Bag II. The ball so drawn is found to be black in colour. Then the probability, that the transferred ball is red, is:

(A) 
$$\frac{4}{9}$$
 (B)  $\frac{5}{18}$  (C)  $\frac{1}{6}$  (D)  $\frac{3}{10}$ 

Official Ans. by NTA (B)

	3R	2R
Sol.	4B	5B
	3W	 2W

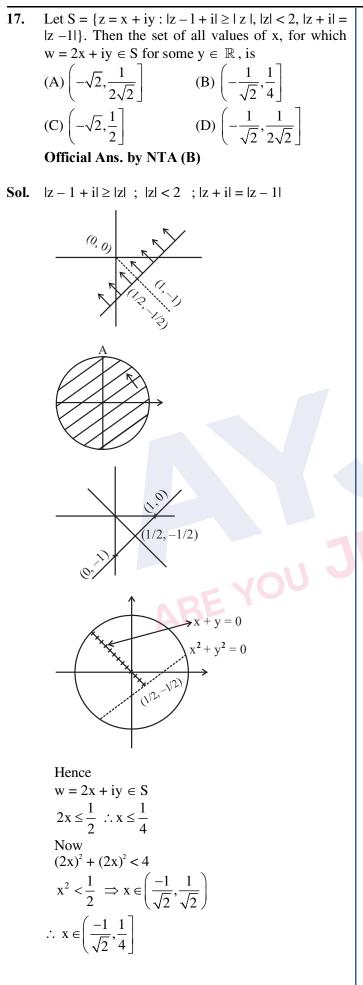
A : Drown ball from boy II is black

B : Red ball transferred

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$
3 5

$$=\frac{\overline{9}^{\times}\overline{10}}{\frac{3}{9}\times\frac{5}{10}+\frac{4}{9}\times\frac{6}{10}+\frac{3}{9}\times\frac{5}{10}}$$
$$=\frac{15}{15+24+15}=\frac{15}{54}=\frac{5}{18}$$

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**18.** Let  $\vec{a}, \vec{b}, \vec{c}$  be three coplanar concurrent vectors such that angles between any two of them is same. If the product of their magnitudes is 14 and  $(\vec{a} \times \vec{b}).(\vec{b} \times \vec{c}) + (\vec{b} \times \vec{c}).(\vec{c} \times \vec{a}) + (\vec{c} \times \vec{a}).(\vec{a} \times \vec{b}) = 168$ then  $|\vec{a}| + |\vec{b}| + |\vec{c}|$  is equal to:

(C) 16 (D) 18

Official Ans. by NTA (C)

**Sol.**  $\|\vec{a}\| \|\vec{b}\| \|\vec{c}\| = 14$ 

$$\vec{a} \wedge \vec{b} = \vec{b} \wedge \vec{c} = \vec{c} \wedge \vec{a} = \theta = \frac{2\pi}{3}$$
So,  $\vec{a}.\vec{b} = -\frac{1}{2}ab$ ,  $\vec{b}.\vec{c} = -\frac{1}{2}bc$ ,  $\vec{a}.\vec{c}. = -\frac{1}{2}ac$ 
(let)
 $(\vec{a} \times \vec{b}).(\vec{b} \times \vec{c}) = (\vec{a}.\vec{b})(\vec{b}.\vec{c}) - (\vec{a}.\vec{c})(\vec{b}.\vec{b})$ 
 $= \frac{1}{4}ab^{2}c + \frac{1}{2}ab^{2}c = \frac{3}{4}ab^{2}c$ 
Similarly
 $(\vec{b} \times \vec{c}).(\vec{c} \times \vec{a}) = \frac{3}{4}abc^{2}$ 
 $(\vec{c} \times \vec{a}).(\vec{a} \times \vec{b}) = \frac{3}{4}a^{2}bc$ 
 $168 = \frac{3}{4}abc(a + b + c)$ 
So,  $(a + b + c) = 16$ 
19. The domain of the function
 $f(x) = \sin^{-1}\left(\frac{x^{2} - 3x + 2}{x^{2} + 2x + 7}\right)$  is :
(A)  $[1, \infty)$  (B)  $(-1, 2]$ 
(C)  $[-1, \infty)$  (D)  $(-\infty, 2]$ 
Official Ans. by NTA (C)
Sol.  $f(x) = \sin^{-1}\left(\frac{x^{2} - 3x + 2}{x^{2} + 2x + 7}\right)$  Domain
 $\frac{x^{2} - 3x + 2}{x^{2} + 2x + 7} \ge -1$  and  $\frac{x^{2} - 3x + 2}{x^{2} + 2x + 7} \le 1$ 
 $2x^{2} - x + 9 \ge 0$  and  $5x \ge -5 \Longrightarrow x \ge -1$ 
 $x \in \mathbb{R}$ 

Hence Domain  $x \in [-1, \infty)$ 



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 $(p \Rightarrow q) \lor (p \Rightarrow r)$  is NOT 20. The statement equivalent to: (A)  $(p \land (\sim r)) \Rightarrow q$  (B)  $(\sim q) \Rightarrow ((\sim r) \lor p)$ (D)  $(p \land (\sim q)) \Rightarrow r$ (C)  $p \Rightarrow (q \lor r)$ 

Official Ans. by NTA (B)

**Sol.**  $(p \rightarrow q) \lor (p \rightarrow r)$  $(\sim p \lor q) \lor (\sim p \lor r)$  $= \sim p \lor (q \lor r)$  $= p \rightarrow (q \lor r) \equiv (3)$  is true. Now (1)  $(p \land \sim r) \rightarrow q$ 

> $\sim$ (p  $\wedge \sim$  r)  $\lor$  q = ( $\sim$ p  $\lor$  r)  $\lor$  q  $= \sim p \lor (r \lor q) = p \to (q \lor r)$ (4)  $(p \land \sim q) \rightarrow r = p \rightarrow (q \lor r)$

#### **SECTION-B**

1. The sum and product of the mean and variance of a 82.5 binomial distribution are and 1350 respectively. They the number of trials in the binomial distribution is:

Official Ans. by NTA (96)

- Sol. Let, mean = m = np& variance = v = npq, p + q = 1 $Sum = m + v = \frac{165}{2}$ Product = mv = 1350On solving, m = np = 60 & v = npq =  $\frac{45}{2}$   $\therefore$  q =  $\frac{3}{8}$   $\therefore$  P =  $\frac{5}{8}$ Hence n = 96
- 2. Let  $\alpha$ ,  $\beta$  ( $\alpha > \beta$ ) be the roots of the quadratic equation  $x^2-x-4=0.$  If  $P_{_n}=\alpha^{^n}-\beta^{^n}\!,\,n\in\mathbb{N}$  , then

$$\frac{P_{15}P_{16} - P_{14}P_{16} - P_{15}^2 + P_{14}P_{15}}{P_{13}P_{14}} \text{ is equal to} \_\_\_.$$

Official Ans. by NTA (16)

Sol. 
$$Pn = \alpha^{n} - \beta^{n}$$
  
 $\frac{P_{15}P_{16} - P_{14}P_{16} - P_{15}^{2} + P_{14}P_{15}}{P_{13}P_{14}}$  (1)  
As  $P_{n} - P_{n-1} = (\alpha^{n} - \beta^{n}) - (\alpha^{n-1} - \beta^{n-1})$   
 $= \alpha^{n-2}(\alpha^{2} - \alpha) - \beta^{n-2}(\beta^{2} - \beta)$   
 $= 4(\alpha^{n-2} - \beta^{n-2})$   
 $P_{n} - P_{n-1} = 4P_{n-2}$   
Hence Expression (1)  
 $\frac{P_{16}(P_{15} - P_{14}) - P_{15}(P_{15} - P_{14})}{P_{13}P_{14}}$   
 $= \frac{(P_{15} - P_{14})(P_{16} - P_{15})}{P_{13}P_{14}} = \frac{(4P_{13})(4P_{14})}{P_{13}P_{14}} = 16$   
3. Let  $x = \begin{bmatrix} 1\\ 1\\ 1 \end{bmatrix}$  and  $A = \begin{bmatrix} -1 & 2 & 3\\ 0 & 1 & 6\\ 0 & 0 & -1 \end{bmatrix}$ . For  $k \in \mathbb{N}$ , if

X'  $A^{k}$  X = 33, then k is equal to:

Official Ans. by NTA (10)

3.

$$\begin{aligned} \mathbf{A} &= \begin{bmatrix} 1\\1\\1 \end{bmatrix}; \ \mathbf{A} = \begin{bmatrix} -12 & 3\\0 & 1 & 6\\0 & 0 & -1 \end{bmatrix} \\ \mathbf{X}^{\mathsf{T}} \mathbf{A}^{\mathsf{K}} \mathbf{X} &= 33 \\ \begin{bmatrix} 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 2 & 3\\0 & 1 & 6\\0 & 0 & -1 \end{bmatrix}^{\mathsf{K}} \begin{bmatrix} 1\\1\\1 \end{bmatrix} = 33 \\ \begin{bmatrix} 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 2 & 3\\0 & 1 & 6\\0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 1\\1\\1 \end{bmatrix} = 33 \\ \mathbf{A} \\ \mathbf{A} \\ \mathbf{A} \\ \mathbf{A}^{2} &= \begin{bmatrix} -12 & 3\\0 & 1 & 6\\0 & 0 & -1 \end{bmatrix} \begin{bmatrix} -12 & 3\\0 & 1 & 6\\0 & 0 & -1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 6\\0 & 1 & 0\\0 & 0 & 1 \end{bmatrix} \\ \mathbf{A}^{4} &= \begin{bmatrix} 1 & 0 & 6\\0 & 1 & 0\\0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 6\\0 & 1 & 0\\0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 12\\0 & 1 & 0\\0 & 0 & 1 \end{bmatrix} \\ \mathbf{A}^{8} &= \begin{bmatrix} 1 & 0 & 24\\0 & 1 & 0\\0 & 0 & 1 \end{bmatrix} \end{aligned}$$

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$$A^{10} = \begin{bmatrix} 1 & 0 & 6 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 24 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 30 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
  
for K  $\rightarrow$  Even A<sup>K</sup> =  $\begin{bmatrix} 1 & 0 & 3K \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   
X<sup>T</sup>A<sup>K</sup>X = 33 (This is not correct)  
[1 1 1]  $\begin{bmatrix} 1 & 0 & 3K \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$   
= [1 1 3K+1]  $\begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$  = [3K+3]  
 $\therefore$  3K + 3 = 33  $\therefore$  K = 10  
But it should be dropped as 33 is n

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But it should be dropped as 33 is not matrix If K is odd  $X^{T}A^{K}X = 33$   $X^{T}AA^{K-1}X = 33$   $\begin{bmatrix} 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -1 & 2 & 3 \\ 0 & 1 & 6 \\ 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 3k-3 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 33$   $\begin{bmatrix} -1 & 3 & 8 \end{bmatrix} \begin{bmatrix} 3k-2 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 33 \end{bmatrix}$   $\begin{bmatrix} -3k+13 \end{bmatrix} = \begin{bmatrix} 33 \end{bmatrix}$ k = 20/3 (not possible)

The number of natural numbers lying between 1012 and 23421 that can be formed using the digits 2, 3, 4, 5, 6 (repetition of digits is not allowed) and divisible by 55 is\_\_\_\_,

### Official Ans. by NTA (6)

**Sol.** 4 digit numbers

For divisibility by 55, no. should be

div. by 5 and 11 both Also, for divisibility by 11 a b c d

$$a + c = b + 5$$
  
for b = 1 a = 2, c = 4  
a = 4, c = 2  
for b = 2 a = 3, c = 4  
a = 4, c = 3  
for b = 3 a = 6, c = 2  
a = 2, c = 6

- $\therefore$  6 possible four digit no.s are div. by 55
- (II) 5 digit number is not possible

5. If 
$$\sum_{k=1}^{10} K^2 (10_{C_K})^2 = 22000L$$
, then L is equal to \_\_\_\_\_.

Official Ans. by NTA (221)

Sol. 
$$\sum_{K=1}^{10} K^{2} {\binom{10}{C_{K}}}^{2}$$
$$\sum_{K=1}^{10} {\binom{K}{.}^{10}C_{K}}^{2} = \sum_{K=1}^{10} {\binom{10.9}{C_{K-1}}}^{2}$$
$$= 100 \sum_{K=1}^{10.9} C_{K-1} \cdot {}^{9}C_{10-K}$$
$$= 100 {\binom{18}{C_{9}}} = 100 {\binom{18!}{9!9!}}$$
$$\Rightarrow 4862000 = 22000L$$
Hence L = 221  
6. If [t] denotes the greatest integer < 1

If [t] denotes the greatest integer  $\leq$  t, then number of points, at which the function f(x) = 4 | 2x + 3| + $9 \left[ x + \frac{1}{2} \right] - 12 [x + 20]$  is not differentiable in the open interval (-20, 20), is\_\_\_\_.

Official Ans. by NTA (79)

Sol.  $f(x) = 4l2x + 3l + 9\left[x + \frac{1}{2}\right] - 12[x + 20]$   $x \in (-20, 20)$  f(x) is not Diff. at  $x = I \in \{-19, -18, ..., 0, ..., 19\} = 39$ at  $x = I + \frac{1}{2}$ , f(x) Non diff. at 39 points Check at  $x = \frac{-3}{2}$  Discount at  $x = \frac{-3}{2}$   $\therefore$  N. R(1)

No. of point of non-differentiabilty

$$= 39 + 39 + 1 = 79$$



7. If the tangent to the curve  $y = x^3 - x^2 + x$  at the point (a, b) is also tangent to the curve  $y = 5x^2 + 2x - 25$  at the point (2, -1), then |2a + 9b| is equal to \_\_\_\_\_.

Official Ans. by NTA (195)

**Sol.**  $y = 5x^2 + 2x - 25$ P(2, -1)y' = 10x + 2 $y'_{P} = 22$ ∴ tangent to curve at P y + 1 = 22 (x - 2)y = 22x - 45 $y = x^{3} - x^{2} + x$ Q(a,b) $\frac{dy}{dx}\Big|_{C_2} = 3x^2 - 2x + 1$  $\frac{dy}{dx}\Big|_{\Omega} = 3a^2 - 2a + 1$ Hence  $3a^2 - 2a + 1 = 22$  $\therefore 3a^2 - 2a - 21 = 0$  $3a^2 - 9a + 7a - 21 = 0$ (3a+7)(a-3) = 0from curve  $b = a^3 - a^2 + a$ a = 3b = 21|2a + 9b| = 195at a = -7/3 tangent will be parallel Hence it is rejected

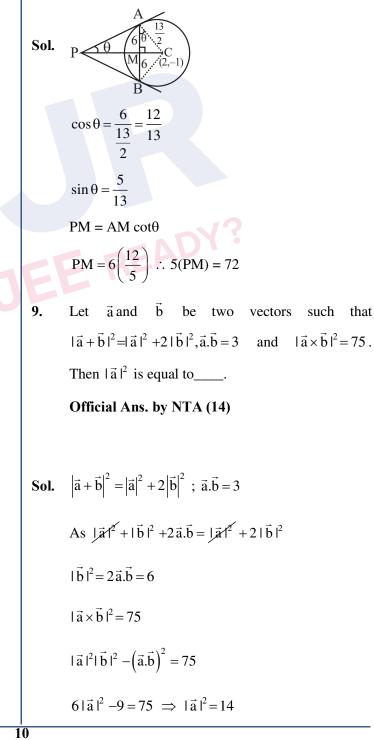
Let AB be a chord of length 12 of the circle

$$(x-2)^{2} + (y+1)^{2} = \frac{169}{4}.$$

8.

If tangents drawn to the circle at points A and B intersect at the point P, then five times the distance of point P from chord AB is equal to \_\_\_\_.

Official Ans. by NTA (72)



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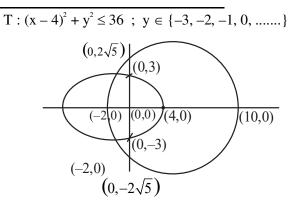
10. Let

$$S = \left\{ (x, y) \in \mathbb{N} \times \mathbb{N} : 9(x - 3)^2 + 16(y - 4)^2 \le 144 \right\}$$
  
and 
$$T = \left\{ (x, y) \in \mathbb{R} \times \mathbb{R} : (x - 7)^2 + (y - 4)^2 \le 36 \right\}.$$

The  $n(S \cap T)$  is equal to\_\_\_\_\_.

Official Ans. by NTA (27)

Sol. S:  $\frac{(x-3)^2}{16} + \frac{(y-4)^2}{9} \le 1$ ; x, y  $\in \{1, 2, 3, \dots\}$ T:  $(x-7)^2 + (y-4)^2 \le 36$  x, y  $\in \mathbb{R}$ Let x-3 = x : y-4 = yS:  $\frac{x^2}{16} + \frac{y^2}{9} \le 1$ ;  $x \in \{-2, -1, 0, 1, \dots\}$ 



 $S \cap T = (-2, 0), (-1, 0), \dots (4, 0) \rightarrow (7)$ (-1, 1), (0, 1), \dots (3, 1)  $\rightarrow (5)$ (-1, -1), (0, -1), \dots (3, -1)  $\rightarrow (5)$ (-1, 2), (0, 2), (1, 2), (2, 2)  $\rightarrow (4)$ (-1, -2), (0, -2), (1, -2), (2, -2)  $\rightarrow (4)$ (0, 3) (0, -3)  $\rightarrow (2)$ 

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