

FINAL JEE-MAIN EXAMINATION - JULY, 2022

(Held On Friday 29th July, 2022)

TIME:9:00 AM to 12:00 NOON

PHYSICS

SECTION-A

1. Given below are two statements : One is labelled as Assertion (A) and other is labelled as

Reason (R).

Assertion (A) : Time period of oscillation of a liquid drop depends on surface tension (S), if density of the liquid is p and radius of the drop is r,

then $T = k \sqrt{\frac{pr^3}{s^{3/2}}}$ is dimensionally correct,

where K is dimensionless.

Reason (R) : Using dimensional analysis we get R.H.S. having different dimension than that of time period.

In the light of above statements, choose the correct answer from the options given below.

(A) Both (A) and (R) are true and (R) is the correct explanation of (A)

(B) Both (A) and (R) are true but (R) is not the correct explanation of (A)

(C) (A) is true but (R) is false

(D) (A) is false but (R) is true

Official Ans. by NTA (D)

Sol.
$$T = k$$

Dimensions of RHS = $\frac{\left[M^{\frac{1}{2}}L^{-\frac{3}{2}}\right]\left[L^{\frac{3}{2}}\right]}{\left[MT^{-2}\right]^{\frac{3}{4}}} = M^{\frac{1}{8}} L^{0} T^{\frac{3}{2}}$

Dimensions of L.H.S \neq Dimensions of R.H.S

 \therefore option (D)

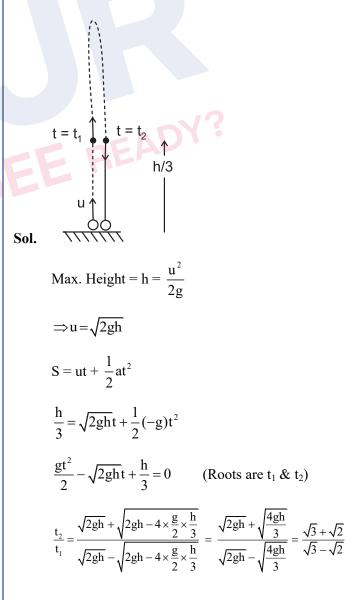
TEST PAPER WITH SOLUTION

 A ball is thrown up vertically with a certain velocity so that, it reaches a maximum height h. Find the ratio of the times in which it is at height

 $\frac{h}{3}$ while going up and coming down respectively.

(A)
$$\frac{\sqrt{2}-1}{\sqrt{2}+1}$$
 (B) $\frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}$
(C) $\frac{\sqrt{3}-1}{\sqrt{3}+1}$ (D) $\frac{1}{3}$

Official Ans. by NTA (B)





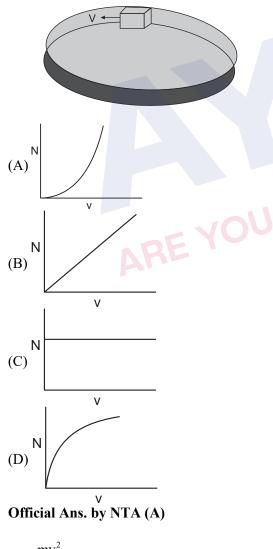
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3. If
$$t = \sqrt{x} + 4$$
, then $\left(\frac{dx}{dt}\right)_{t=4}^{t=4}$ is:
(A) 4 (B) Zero
(C) 8 (D) 16
Official Ans. by NTA (B)

Sol.
$$t = \sqrt{x} + 4$$

 $\Rightarrow x = (t - 4)^2 = t^2 - 8t + 16$
 $\Rightarrow \frac{dx}{dt} = 2t - 8$
 $\Rightarrow \frac{dx}{dt}\Big|_{t=4} = 2 \times 4 - 8 = 0$

4. A smooth circular groove has a smooth vertical wall as shown in figure. A block of mass m moves against the wall with a speed v. Which of the following curve represents the correct relation between the normal reaction on the block by the wall (N) and speed of the block (v) ?



Sol. N = $\frac{mv^2}{r}$

Curve is parabola $Y = kx^2$ 5. A ball is projected with kinetic energy E, at an angle of 60° to the horizontal. The kinetic energy of this ball at the highest point of its flight will become :

(A) Zero (B)
$$\frac{E}{2}$$

(C)
$$\frac{E}{4}$$
 (D) E

Official Ans. by NTA (C)

60 Sol.

$$E = \frac{1}{2}mu^2$$

6.

At Highest point, Velocity V = $u \cos 60^\circ = \frac{u}{2}$

ucos60

- \therefore K.E at topmost point = $\frac{1}{2}m\left(\frac{u}{2}\right)^2 = \frac{E}{4}$
- Two bodies of mass 1 kg and 3 kg have position vectors $\hat{i} + 2\hat{j} + \hat{k}$ and $-3\hat{i} - 2\hat{j} + \hat{k}$ respectively. The magnitude of position vector of centre of mass of this system will be similar to the magnitude of vector :

(A)
$$\hat{i} - 2\hat{j} + \hat{k}$$
 (B) $-3\hat{i} - 2\hat{j} + \hat{k}$

(C)
$$-2\hat{i}+2\hat{k}$$
 (D) $-2\hat{i}-\hat{j}+2\hat{k}$

Official Ans. by NTA (A)

Sol.
$$\vec{r}_{com} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2}{m_1 + m_2} = \frac{1(\hat{i} + 2\hat{j} + \hat{k}) + 3(-3\hat{i} - 2\hat{j} + \hat{k})}{1 + 3}$$

$$= -2\hat{i} - \hat{j} + \hat{k}$$
$$|2\hat{i} - \hat{j} + \hat{k}| = \sqrt{(2)^2 + (1)^2 + (1)^2} = \sqrt{6}$$

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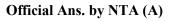
7. Given below are two statements : One is labelled as Assertion (A) and the other is labelled as Reason (R).

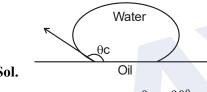
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Assertion (A) : Clothes containing oil or grease stains cannot be cleaned by water wash.

Reason (R) : Because the angle of contact between the oil/ grease and water is obtuse. In the light of the above statements, choose the correct answer from the option given below.

- (A) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (B) Both (A) and (R) are true but (R) is not the correct explanation of (A)
- (C) (A) is true but (R) is false
- (D)(A) is true but (R) is true





Sol.

 $\theta c > 90^{\circ}$

For water oil interface

8. If the length of a wire is made double and radius is halved of its respective values. Then, the Young's modules of the material of the wire will :

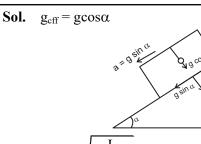
(A) Remains same

- (B) Become 8 times its initial value
- (C) Become $\frac{1^m}{4}$ of its initial value

(D) Become 4 times its initial value Official Ans. by NTA (A)

- Sol. Y depends on material of wire
- The time period of oscillation of a simple 9. pendulum of length L suspended from the roof of a vehicle, which moves without friction down an inclined plane of inclination α , is given by :

(A)
$$2\pi\sqrt{L/(g\cos\alpha)}$$
 (B) $2\pi\sqrt{L/(g\sin\alpha)}$
(C) $2\pi\sqrt{L/g}$ (D) $2\pi\sqrt{L/(g\tan\alpha)}$
Official Ans. by NTA (A)



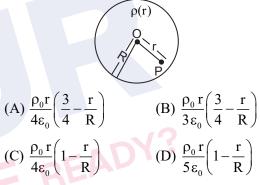
gcosα

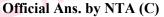
 $T = 2\pi$

10. A spherically symmetric charge distribution is considered with charge density varying as

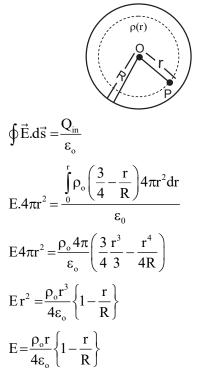
$$\rho(\mathbf{r}) = \begin{cases} \rho_0 \left(\frac{3}{4} - \frac{\mathbf{r}}{\mathbf{R}} \right) & \text{for } \mathbf{r} \le \mathbf{R} \\ \text{Zero} & \text{for } \mathbf{r} > \mathbf{R} \end{cases}$$

Where, r(r < R) is the distance from the centre O (as shown in figure). The electric field at point P will be :





By Gauss law Sol.





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11. Given below are two statements.

Statement I : Electric potential is constant within and at the surface of each conductor.

Statement II : Electric field just outside a charged conductor is perpendicular to the surface of the conductor at every point.

In the light of the above statements, choose the most appropriate answer from the options give below.

- (A) Both statement I and statement II are correct
- (B) Both statement I and statement II are incorrect
- (C) Statement I is correct but statement II is incorrect
- (D) Statement I is incorrect but and statement II is correct

Official Ans. by NTA (A)

Sol. (Properties of conductor)

Statement – I, true as body of conductor acts as equipotential surface.

Statement – 2 True, as conductor is equipotential. Tangential component of electric field should be zero. Therefore electric field should be perpendicular to surface.

12. Two metallic wires of identical dimensions are connected is series. If σ_1 and σ_2 are the conductivities of the these wires respectively, the effective conductivity of the combination is :

(A)
$$\frac{\sigma_1 \sigma_2}{\sigma_1 + \sigma_2}$$
 (B) $\frac{2\sigma_1 \sigma_2}{\sigma_1 + \sigma_2}$

(C)
$$\frac{\sigma_1 + \sigma_2}{2\sigma_1\sigma_2}$$
 (D) $\frac{\sigma_1 + \sigma_2}{\sigma_1\sigma_2}$

Official Ans. by NTA (B)

$$\begin{array}{ccc} A(\underbrace{) & \sigma_1 & (\underbrace{)} & \sigma_2 \\ \ell & \ell \end{array} & \equiv & \underbrace{(\underbrace{)} & \sigma_{eq} \\ 2\ell \end{array}} A \end{array}$$

Let length of wire be ' ℓ '

Area of wire as 'A'

For equivalent wire length = 2ℓ & area will be A

Thermal resistance

$$R_{eq} = R_1 + R_2$$

$$\frac{2\ell}{\sigma_{eq}A} = \frac{\ell}{\sigma_1A} + \frac{\ell}{\sigma_1A}$$

$$\frac{2\ell}{\sigma_{eq}} = \frac{\ell}{\sigma_1} + \frac{\ell}{\sigma_2} \implies \sigma_{eq} = \frac{2\sigma_1\sigma_2}{\sigma_1 + \sigma_2}$$

13. An alternating emf E = 440 sin 100 π t is applited to a circuit containing an inductance of $\frac{\sqrt{2}}{\pi}$ H. If an a.c. ammeter is connected in the circuit, its reading will be :

> (A) 4.4 A (B) 1.55 A (C) 2.2 A (D) 3.11 A

Official Ans. by NTA (C)

Sol. E = 440 Sin100
$$\pi$$
t, L = $\frac{\sqrt{2}}{\pi}$ H

$$X_{L} = \omega L = 100 \pi \frac{\sqrt{2}}{\pi} = 100 \sqrt{2} \Omega$$

Peak current
$$I_0 = \frac{E_0}{X_L} = \frac{440}{100\sqrt{2}} = 2.2\sqrt{2} \text{ A}$$

AC ammeter reads RMS value therefore reading will be I_{rms}

$$I_{\rm rms} = \frac{I_0}{\sqrt{2}} = 2.2 \text{ A}$$

- 14. A coil of inductance 1 H and resistance 100 Ω is connected to a battery of 6 V. Determine approximately :
 - (a) The time elapsed before the current acquires half of its steady state value

(b) The energy stored in the magnetic field associated with the coil at an instant 15 ms after the circuit is switched on. (Given In2 = 0.693, $e^{-3/2} = 0.25$)

$$(A) t = 10 ms; U = 2 mJ$$

- (B) t = 10 ms; U = 1 mJ
- (C) t = 7 ms; U = 1 mJ
- (D) t = 7 ms; U = 2 mJ

Official Ans. by NTA (C)

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Sol. Given circuit is R - L growth circuit $R = 100\Omega$ L = 1H ME = 6v

$$i = \frac{E}{R} (1 - e^{-t/\tau})$$
$$i = \frac{E}{R} = \frac{E}{R} (1 - e^{-t/\tau})$$

2R R⁽¹⁾

Solving $t = \tau \ln 2$

$$t = \frac{1}{R} \ln 2 = \frac{1}{100} \ 0.693 = 0.00693$$
$$= 7 \ \text{ms}$$

$$i(15ms) = \frac{E}{R}(1 - e^{-\frac{15}{10}})$$
$$i = \frac{6}{100}(1 - \frac{1}{4}) = \frac{3}{4} \times \frac{6}{100}$$
$$U = \frac{1}{2}LI^{2},$$

by solving we get U = 1 mJ.

Match List – I with List – II

15.

List – I	List - II	
(a) UV rays	(i) Diagnostic tool in	
	medicine	
(b) X-rays (ii) Water purification		
(c) Microwave	(iii) Communication, Radar	
(d) Infrared wave	(iv) Improving visibility in	
	foggy days	

Choose the correct answer from the options given below :

(A) (a)-(iii), (b)-(ii), (c)-(i), (d)-(iv)
(B) (a)-(ii), (b)-(i), (c)-(iii), (d)-(iv)
(C) (a)-(ii), (b)-(iv), (c)-(iii), (d)-(i)
(D) (a)-(iii), (b)-(i), (c)-(ii), (d)-(iv)
Official Ans. by NTA (B)

Sol. (a) uv rays – used for water purification

- (b) x-rays used for diagnosing fracture
- (c) Microwaves are used for mobile and radar communication
- (d) Infrared waves show less scattering therefore used in foggy days

$$(a-ii), (b-i), (c-iii), (d-iv)$$

16. The kinetic energy of emitted electron is E when the light incident on the metal has wavelength λ. To double the kinetic energy, the incident light must have wavelength :

(A)
$$\frac{hc}{E\lambda - hc}$$
 (B) $\frac{hc\lambda}{E\lambda + hc}$
(C) $\frac{h\lambda}{E\lambda + hc}$ (D) $\frac{hc\lambda}{E\lambda - hc}$

Official Ans. by NTA (B)

Sol.
$$E = \frac{hc}{\lambda} - \phi - (i)$$
$$2E = \frac{hc}{\lambda'} - \phi - (ii)$$
$$(ii) - (i)$$
$$E = hc \left(\frac{1}{\lambda'} - \frac{1}{\lambda}\right)$$
$$\Rightarrow \lambda' = \frac{hc\lambda}{E\lambda + hc}$$

17. Find the ratio of energies of photons produced due to transition of an election of hydrogen atom from its(i) second permitted energy level to the first level, and (ii) the highest permitted energy level to the first permitted level.

Official Ans. by NTA (A)

Sol.
$$E_n = \frac{-13.6}{n^2} ev$$

 $\Rightarrow \frac{E_2 - E_1}{E_\infty - E_1} = \frac{13.6(1 - \frac{1}{4})}{13.6} = \frac{3}{4}$

18. Find the modulation index of an AM wave having8 V variation where maximum amplitude of the AM wave is 9 V.

Sol. Modulation index: $m = \frac{A_m}{A_c}$

Given
$$2A_m = 8$$

 $A_m + A_c = 9 \implies A_c = 5$
 $\therefore m = \frac{4}{5} = 0.8$



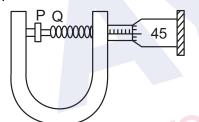
19. A travelling microscope has 20 divisions per cm on the main scale while its Vernier scale has total 50 divisions and 25 Vernier scale divisions are equal to 24 main scale divisions, what is the least count of the travelling microscope ?

(A) 0.001 cm
(B) 0.002 mm
(C) 0.002 cm
(D) 0.005 cm

Official Ans. by NTA (C)

Sol. 1 MSD =
$$\frac{1}{20}$$
 cm
1 VSD = $\frac{24}{25}$ MSD = $\frac{24}{25} \times \frac{1}{20}$ cm
∴ Least count = $\frac{1}{20} \left(1 - \frac{24}{25}\right)$ cm
= $\frac{1}{20} \times \frac{1}{25} = \frac{1}{500}$ cm
= 0.002 cm

20. In an experiment to find out the diameter of wire using screw gauge, the following observation were noted :



- (a) Screw moves 0.5 mm on main scale in one complete rotation
- (b) Total divisions on circular scale = 50
- (c) Main scale reading is 2.5 mm
- (d) 45th division of circular scale is in the pitch line
- (e) Instrument has 0.03 mm negative error

Then the diameter of wire is :

(A) 2.92 mm	(B) 2.54 mm
-------------	-------------

- (C) 2.98 mm (D) 3.45 mm
- Official Ans. by NTA (C)

Sol. MSR = 2.5 mm

 $CSR = 45 \times \frac{0.5}{50} \text{ mm}$ = 0.45 mm Diameter reading = MSR + CSR - zero error = 2.5 + 0.45 - (-0.03) = 2.98 mm

SECTION-B

An object is projected in the air with initial velocity u at an angle θ. The projectile motion is such that the horizontal range R, is maximum. Another object is projected in the air with a horizontal range half of the range of first object. The initial velocity remains same in both the case. The value of the angle of projection, at which the second object is projected, will be _____degree.

Official Ans. by NTA (15)

ol.
$$R_{max} = \frac{u^2 \sin 2(45^\circ)}{g} = \frac{u^2}{g}$$
$$\frac{R}{2} = \frac{u^2}{2g} = \frac{u^2 \sin 2\theta}{g}$$
$$\sin 2\theta = \frac{1}{2}$$
$$2\theta = 30^\circ, 150^\circ$$
$$\theta = 15^\circ, 75^\circ$$
Ans. 15, 75

S

2. If the acceleration due to gravity experienced by a point mass at a height h above the surface of earth is same as that of the acceleration due to gravity at a depth α h (h << R_e) from the earth surface. The value of α will be _____.

(use $R_e = 6400 \text{ km}$)

Official Ans. by NTA (2)

Sol.
$$g\left(1-\frac{2h}{R}\right)=g\left(1-\frac{d}{R}\right)$$

 $\frac{2h}{R}=\frac{d}{R}$
 $\alpha h=d$
 $\alpha=2$

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The pressure P₁ and density d₁ of diatomic gas 5. The current

 $\left(\gamma = \frac{7}{5}\right)$ changes suddenly to P₂(>P₁) and d₂ respectively during an adiabatic process. The temperature of the gas increases and becomes _______times of its initial temperature.

(given
$$\frac{d_2}{d_1} = 32$$
)

Official Ans. by NTA (4)

Sol.
$$PV^{\gamma} = const$$

 $p\left(\frac{m}{d}\right)^{\gamma} = const$
 $\frac{p}{d^{\gamma}} = const$
 $\frac{p}{d^{\gamma}} = const$
 $\frac{d_2}{d_1} = 32$
 $\frac{p_1}{p_2} = \left(\frac{d_1}{d_2}\right)^{\gamma} = \left(\frac{1}{32}\right)^{\frac{7}{5}} = \frac{1}{128}$
 $\frac{T_1}{T_2} = \frac{P_1V_1}{P_2V_2} = \frac{1}{128}32 = \frac{1}{4}$

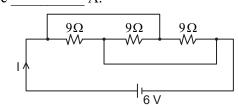
4. One mole of a monoatomic gas is mixed with three moles of a diatomic gas. The molecular specific heat of mixture at constant volume is $\frac{\alpha^2}{4}$ R J/mol K; then the value of α will be _____. (Assume that the given diatomic gas has no vibrational mode.)

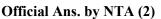
Official Ans. by NTA (3)

Sol.
$$C_v / mix = \frac{n_1 Cv_1 + n_2 Cv_2}{n_1 + n_2}$$

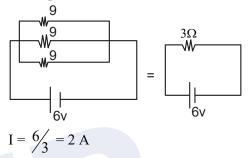
= $\frac{1 \cdot \frac{3R}{2} + 3 \cdot \frac{5R}{2}}{1 + 3}$
= $\frac{9R}{4} = \frac{\alpha^2}{4}R$
 $\alpha = 3$

The current I flowing through the given circuit will be A.





Sol. Equivalent circuit



A closely wounded circular coil of radius 5 cm produces a magnetic field of 37.68 x 10^{-4} T at its center. The current through the coil is ______ A. [Given, number of turns in the coil is 100 and $\pi = 3.14$]

Official Ans. by NTA (3)

Sol.
$$B_{\text{centre}} = \frac{N\mu_0 l}{2R}$$

 $37.68 \times 10^{-4} = \frac{100 \times 4\pi \times 10^{-7} \times 1}{2 \times 5 \times 10^{-2}}$

I = 3A

6.

Two light beams of intensities 4I and 9I interfere on a screen. The phase difference between these beams on the screen at point A is zero and at point B is π. The difference of resultant intensities, at the point A and B, will be _____ I.

Official Ans. by NTA (24)

Sol.
$$I_{net} = I_1 + I_2 + 2 \sqrt{I_1} \sqrt{I_2} \cos \phi$$

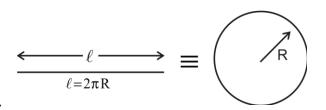
 I_{max} for $\phi = 0 \& I_{min}$ for $\phi = \pi$
 $I_{max} = \left(\sqrt{I_1} + \sqrt{I_2}\right)^2 = \left(\sqrt{9I} + \sqrt{4I}\right)^2 = 25 I$
 $I_{min} = \left(\sqrt{I_1} - \sqrt{I_2}\right)^2 = \left(\sqrt{9I} - \sqrt{4I}\right)^2 = I$
 $I_{max} - I_{min} = 25 I - I = 24 I$



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8. A wire of length 314 cm carrying current of 14 A is bent to form a circle. The magnetic moment of the coil is _____ A-m². [Given $\pi = 3.14$]

Official Ans. by NTA (11)



Sol.

 $\frac{314}{100} = 2\pi R$ R = 0.5 m

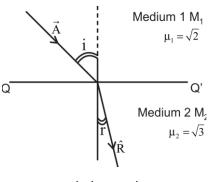
Magnetic Moment = IA

$$= 14 \times \pi R^{2}$$
$$= 14 \times (3.14) \times \frac{1}{4}$$
$$= 10.99 \approx 11.00$$

9. The X-Y plane be taken as the boundary between two transparent media M_1 and M_2 . M_1 in $Z \ge 0$ has a refractive index of $\sqrt{2}$ and M_2 with Z < 0 has a refractive index of $\sqrt{3}$. A ray of light travelling in M_1 along the direction given by the vector $\vec{A} = 4\sqrt{3}\hat{i} - 3\sqrt{3}\hat{j} - 5\hat{k}$, is incident on the plane of separation. The value of difference between the angle of incident in M_1 and the angle of refraction in M_2 will be ______ degree.

Official Ans. by NTA (15)

Sol.
$$\vec{A} = 4\sqrt{3}\hat{i} - 3\sqrt{3}\hat{j} - 5\hat{k}$$



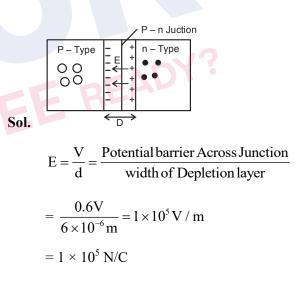
 $\mu_1 \sin i = \mu_2 \sin r$

As incident vector A makes i angle with normal z-axis & refracted vector R makes r angle with normal z – axis with help of direction cosine

$$i = \cos^{-1} \left(\frac{A_z}{A} \right) = \cos^{-1} \left(\frac{5}{\sqrt{(4\sqrt{3})^2 + (3\sqrt{3})^2 + 5^2}} \right)$$
$$= \cos^{-1} \left(\frac{5}{10} \right) \Longrightarrow i = 60^{\circ}$$
$$\sqrt{2} \sin 60 = \sqrt{3} \times \sin r$$
$$r = 45^{\circ}$$
Difference between i& r = 60 - 45 = 15

10. If the potential barrier across a p-n junction is 0.6 V. Then the electric field intensity, in the depletion region having the width of 6×10^{-6} m, will be $\times 10^{5}$ N/C.

Official Ans. by NTA (1)





FINAL JEE-MAIN EXAMINATION - JULY, 2022 (Held On Friday 29th July, 2022) TIME: 9:00 AM to 12:00 NOON **CHEMISTRY TEST PAPER WITH SOLUTION SECTION-A** 3. 100 mL of 5% (w/v) solution of NaCl in water was 1. Which of the following pair of molecules contain prepared in 250 mL beaker. Albumin from the egg odd electron molecule and an expanded octet was poured into NaCl solution and stirred well. molecule? This resulted in a/ an : (A) BCl_3 and SF_6 (B) NO and H₂SO₄ (C) SF₆ and H₂SO₄ (D) BCl₃ and NO (A) Lyophilic sol (B) Lyophobic sol Official Ans. by NTA (B) (C) Emulsion (D) Precipitate Official Ans. by NTA (A) Sol. (A) $BCl_3 \rightarrow Even Electron molecule$ $SF_6 \rightarrow Expanded$ octet molecule (B) NO \rightarrow Odd Electron molecule Standard method for the preparation of lyophilic Sol. $H_2SO_4 \rightarrow Expanded$ octet. sol. (Discussed in lab Manual) (C) $SF_6 \rightarrow Even Electron molecule$ 4. The first ionization enthalpy of Na, Mg and Si, $H_2SO_4 \rightarrow Expanded$ octet. respectively, are: 496, 737 and 786 kJ mol⁻¹. The (D) $BCl_3 \rightarrow Even Electron molecule$ $NO \rightarrow Odd$ Electron molecule first ionization enthalpy (kJ mol⁻¹) of Al is: (A) 487 (B) 768 $\cdot \dot{N} = \dot{O}$: and HO (C) 577 (D) 856 $S \rightarrow 12e^{-}$ in outer orbit. Official Ans. by NTA (C) 2. $N_{2(g)} + 3H_{2(g)} \rightleftharpoons 2NH_{3(g)}$ 20 g 5 g **Sol.** I. E : Na < Al < Mg < Si Consider the above reaction, the limiting reagent of the reaction and number of moles of NH₃ formed ∴ 496 < IE (Al) < 737 respectively are: Option (C), matches the condition. (A) H₂, 1.42 moles (B) H₂, 0.71 moles i.e $IE(AI) = 577 \text{ kJmol}^{-1}$ (C) N₂, 1.42 moles (D) N₂, 0.71 moles Official Ans. by NTA (C) In metallurgy the term "gangue" is used for: 5. (A) Contamination of undesired earthy materials. Sol. $N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$ (B) Contamination of metals, other than desired $W_2 = 20g$ 5g. metal $n = \frac{20}{28} = \frac{5}{2}$ (C) Minerals which are naturally occuring in pure form Stoichiometric Amount: (D) Magnetic impurities in an ore. $N_2 \rightarrow \frac{20/28}{1} = \frac{20}{28}$ $H_2 \rightarrow \frac{5/2}{3} = \frac{5}{6}$ Official Ans. by NTA (A) \therefore N₂ is the Limiting Reagent $\therefore \quad n(NH_3) = 2 \times n(N_2) = 2 \times \frac{20}{28}$ Sol. Earthy and undesired materials present in the ore, other then the desired metal, is known as gangue. = 1.42



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6. The reaction of zinc with excess of aqueous alkali, evolves hydrogen gas and gives :

 $(A) Zn(OH)_2 (B) ZnO$

(C) $[Zn(OH)_4]^{2-}$ (D) $[ZnO_2]^{2-}$

Official Ans. by NTA (D)

Sol. Zinc dissolves in excess of aqueous alkali $Zn + 2OH^{-} + 2H_2O \rightarrow [Zn(OH)_4]^{2-} + H_2 \uparrow$

Tetrahydroxozincate(II) ion

However, this reaction in NCERT is given as

 $Zn + 2 NaOH \rightarrow Na_2 ZnO_2 + H_2 \uparrow$

 ZnO_2^{2-} is anhydrous form of $[Zn(OH)_4]^{2-}$

So in aqueous medium best answer of this question is $[Zn(OH)_4]^{2-}$

7. Lithium nitrate and sodium nitrate, when heated separately, respectively, give :

(A) LiNO₂ and NaNO₂

- (B) Li_2O and Na_2O
- (C) Li₂O and NaNO₂
- (D) LiNO₂ and Na₂O

Official Ans. by NTA (C)

Sol. Li₂O, NaNO₂

As per NCERT Lithium nitrate when heated gives lithium oxide, Li_2O , whereas other alkali metal nitrates decompose to give the corresponding nitrite.

 $4\text{LiNO}_3 \longrightarrow 2\text{Li}_2\text{O} + 4\text{NO}_2 + \text{O}_2$

2NaNO₃ \longrightarrow 2NaNO₂ $+O_2$

However, the decomposition product of $NaNO_3$ are temperature dependent process as shown in the below reaction.

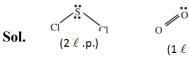
NaNO₃
$$\xrightarrow{\Delta}$$
 NaNO₂ (s) $+\frac{1}{2}$ O₂ (g)
 $\xrightarrow{\Delta} 800^{\circ}C}$
Na₂O (s) $+$ N₂(g) $+$ O₂ (g)

As temperature is not mentioned, we can go by **Ans. (C)**

8. Number of lone pairs of electrons in the central atom of SCl₂, O₃, ClF₃ and SF₆, respectively, are :
(A) 0, 1, 2 and 2
(B) 2, 1, 2 and 0
(C) 1, 2, 2 and 0

(D) 2, 1, 2 and 0

Official Ans. by NTA (B)





- In following pairs, the one in which both transition metal ions are colourless is :
 - (A) Sc^{3+}, Zn^{2+}

9.

- (B) Ti^{4+}, Cu^{2+}
- (C) V^{2+} , Ti^{3+}

(D) Zn^{2+}, Mn^{2+}

Official Ans. by NTA (A)

Sol. (A) Sc^{3+} , Zn^{2+} (B) Ti^{4+} , Cu^{2+} $3d^0 3d^{10} 3d^0 3d^9$ (C) V^{2+} , Ti^{3+} (D) Zn^{2+} , Mn^{2+} $3d^3 3d^1 3d^{10} 3d^5$

No d-d transitions in ions with $d^{\circ} \& d^{10}$ configuration. Therefore they are colourless.

In neutral or faintly alkaline medium, KMnO₄ being a powerful oxidant can oxidize, thiosulphate almost quantitatively, to sulphate. In this reaction overall change in oxidation state of manganese will be :

(A) 5 (B) 1 (C) 0 (D) 3

Official Ans. by NTA (D)

Sol. $8 \overset{+7}{Mn} O_4^{-} + 3S_2 O_3^{2-} + H_2 O \rightarrow 8 \overset{+4}{Mn} O_2 + 6SO_4^{2-} + 2OH^{-}$ Change in oxidation state of Mn is from +7 to +4 which is 3.

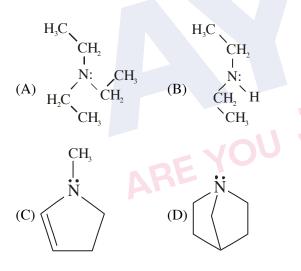
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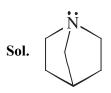
- **11.** Which among the following pairs has only herbicides ?
 - (A) Aldrin and Dieldrin
 - (B) Sodium chlorate and Aldrin
 - (C) Sodium arsinate and Dieldrin
 - (D) Sodium chlorate and sodium arsinite.

Official Ans. by NTA (D)

- **Sol.** Both sodium chlorate and sodium arsenite behave as herbicide.
- **12.** Which among the following is the strongest Bronsted base ?

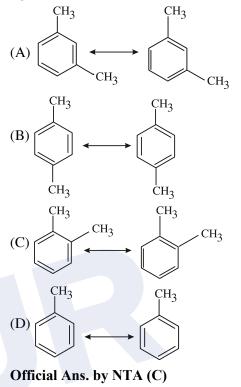


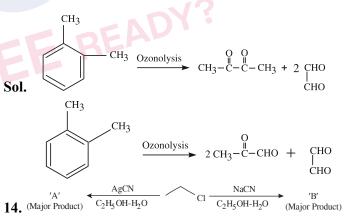
Official Ans. by NTA (D)



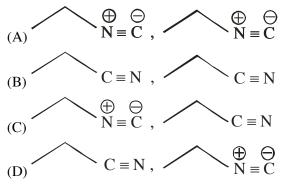
It is most basic because there is no amine inversion.

13. Which among the following pairs of the structures will give different products on ozonolysis? (Consider the double bonds in the structures are rigid and not delocalized.)





Considering the above reactions, the compound 'A' and compound 'B' respectively are :

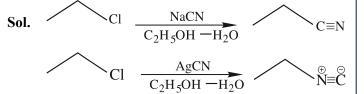


Official Ans. by NTA (C)



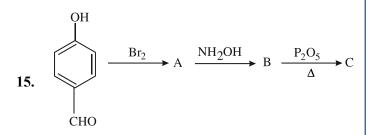
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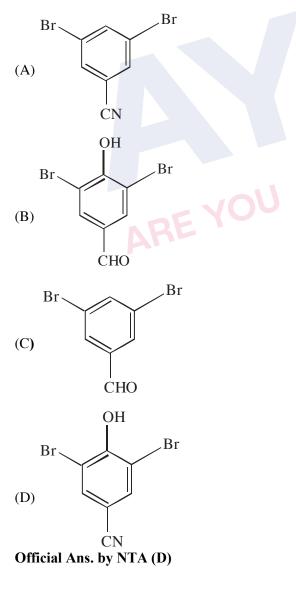
In NaCN; carbon is more nucleophilic atom.

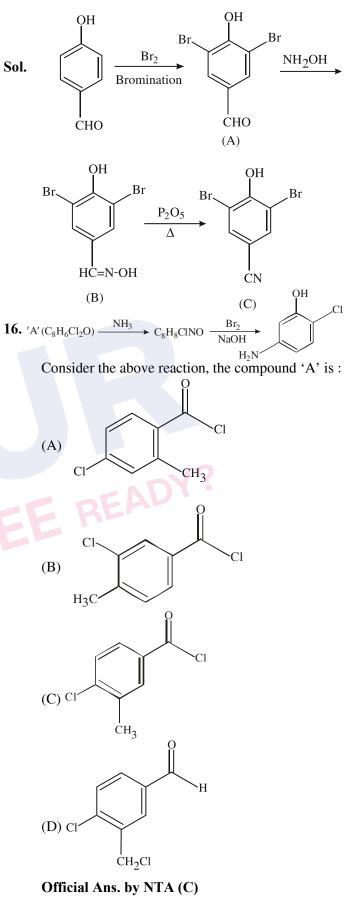
Whereas in AgCN; Ag – C has covalent bond.

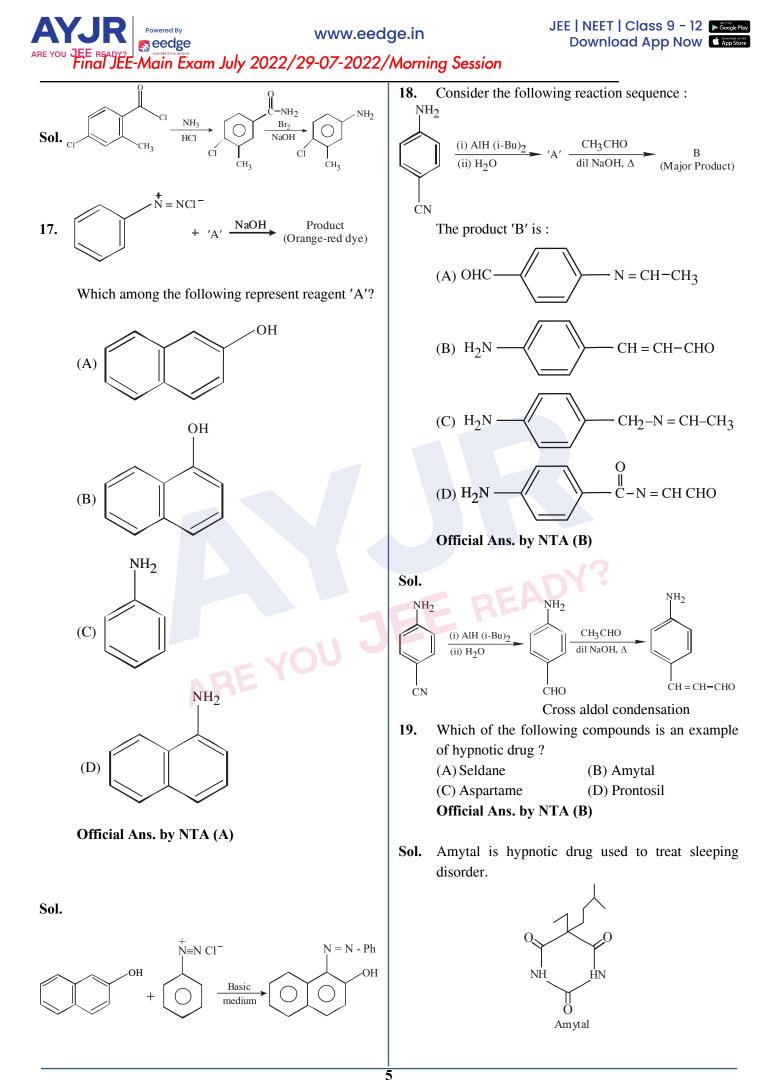


Consider the above reaction sequence, the Product







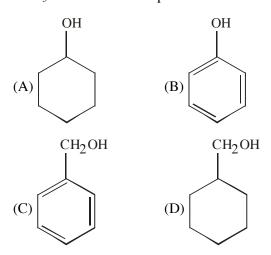


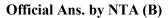
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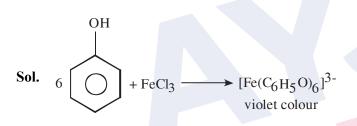
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20. A compound 'X' is acidic and it is soluble in NaOH solution, but insoluble in NaHCO₃ solution.
Compound 'X' also gives violet colour with neutral FeCI₃ solution. The compound 'X' is :







SECTION-B

1. Resistance of a conductivity cell (cell constant 129 m⁻¹) filled with 74.5 ppm solution of KCl is 100 Ω (labelled as solution 1). When the same cell is filled with KCl solution of 149 ppm, the resistance is 50 Ω (labelled as solution 2). The ratio of molar conductivity of solution 1 and solution 2 is i.e.

 $\frac{\wedge_1}{\wedge_2} = x \times 10^{-3}$. The value of x is _____.

(Nearest integer)

Given, molar mass of KCl is 74.5 g mol⁻¹

Official Ans. by NTA (1000)

Sol.
$$\frac{\ell}{\Lambda} = 129 \text{m}^{-1}$$

KCl solution 1:

74.5 ppm, $R_1 = 100 \Omega$

KCl solution 2 :

149 ppm, $R_2 = 50 \Omega$

149 ppm, $R_2 = 50 \Omega$

Here,
$$\frac{\text{ppm}_1}{\text{ppm}_2} = \frac{M_1}{M_2} \left(= \frac{\frac{W_1}{M_0}}{V} \times \frac{V}{\frac{W_2}{M_0}} \right)$$

$$\frac{\Lambda_1}{\Lambda_2} = \frac{\kappa_1 \times \frac{1000}{M_1}}{\kappa_1 \times \frac{1000}{M_1}}$$

 \mathbf{M}_{γ}

$$= \frac{\kappa_1}{\kappa_2} \times \frac{M_2}{M_1}$$

$$=\frac{50}{100}\times 2$$

$$=\frac{\Lambda_1}{\Lambda_2}=1,000\times 10^{-3}$$

Ans. 1,000

2. Ionic radii of cation A⁺ and anion B⁻ are 102 and 181 pm respectively. These ions are allowed to crystallize into an ionic solid. This crystal has cubic close packing for B⁻. A⁺ is present in all octahedral voids. The edge length of the unit cell of the crystal AB is _____ pm. (Nearest Integer)

Official Ans. by NTA (512)

Sol.
$$a = 2(r_+ + r_-)$$

a = 2 (102 + 181)a = 2(283)a = 566 pm

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3. The minimum uncertainty in the speed of an electron in an one dimensional region of length $2a_0$ (Where $a_0 = Bohr radius 52.9 pm$) is _____km s⁻¹. (Given : Mass of electron = 9.1×10^{-31} kg, Planck's constant h = 6.63×10^{-34} Js)

Official Ans. by NTA (548)

Sol. Heisenberg's uncertainty principle

 $\Delta x \times \Delta p_x \ge \frac{h}{4\pi}$

$$\Rightarrow 2a_0 \times m\Delta v_x = \frac{h}{4\pi}$$
(minimum)

$$\Rightarrow \Delta v_x = \frac{h}{4\pi} \times \frac{1}{2a_0} \times \frac{1}{m}$$

$$=\frac{6.63\times10^{-34}}{4\times3.14\times2\times52.9\times10^{-12}\times9.1\times10^{-31}}$$

- $= 548273 \text{ ms}^{-1}$
- $= 548.273 \text{ km s}^{-1}$

$$=$$
 548 km s⁻¹

When 600 mL of 0.2 M HNO₃ is mixed with 4. 400 mL of 0.1M NaOH solution in a flask, the rise in temperature of the flask is $___ \times 10^{-2}$ °C.

(Enthalpy of neutralisation = 57 kJ mo1⁻¹ and

Specific heat of water = $4.2 \text{ JK}^{-1} \text{ g}^{-1}$)

(Neglect heat capacity of flask)

Official Ans. by NTA (54)

Sol. HNO₃ NaOH
600 mL × 0.2 M 400 mL × 0.1 M
= 120 m mol = 40 m mol
HNO₃ + NaOH → NaNO₃ + H₂O
Bef. 120 40
Aft. 80 0 40 m mol

$$\Delta_r$$
H = 40 m mol × (57 × 10³) $\frac{J}{mol}$
= 40 × 10⁻³ mol × 57 × 10³ $\frac{J}{mol}$
= 2280 J
m SΔT = 2280
 \Rightarrow 1000 mL × $\frac{1\text{gm}}{\text{mL}}$ × 4, 2 × ΔT = 2280
 $\Delta T = \frac{2280}{4.2} × 10^{-3}$
= $\frac{22800}{42} × 10^{-3}$
= 542.86 × 10⁻³
 $\Delta T = 54.286 × 10^{-2}$ K
 $\Delta T = 54.286 × 10^{-2}$ C
Ans. 54.286
Answer mentioned as 54 (Closest integer)
5. If O₂ gas is bubbled through water at 303 K

K, the number of millimoles of O_2 gas that dissolve in 1 litre of water is_____. (Nearest Integer) (Given : Henry's Law constant for O₂ at 303 K is 46.82 k bar and partial pressure of $O_2 = 0.920$ bar) (Assume solubility of O2 in water is too small, nearly negligible)

8

Official Ans. by NTA (1)

Sol.
$$p = K_H \times x$$

 $0.920 = 46.82 \times 10^3 \text{ bar} \times \frac{\text{mol of } O_2}{\text{mol of } H_2 O}$

$$0.920 = 46.82 \times 10^{5} \times \frac{\text{mol of O}_{2}}{1000/18}$$
$$0.920 = 46.82 \times n_{o_{2}}$$
$$p = \frac{0.920}{46.82 \times 18} = n_{o_{2}}$$

$$\Rightarrow 1.09 \times 10^{-3} = n_{0_2}$$
$$\Rightarrow m \mod \text{of } \Omega_2 = 1$$

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5.



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6. If the solubility product of PbS is 8×10^{-28} , then the solubility of PbS in pure water at 298 K is $x \times 10^{-16}$ mol L⁻¹. The value of x is _____. (Nearest Integer)

[Given $\sqrt{2} = 1.41$]

Official Ans. by NTA (282)

- Sol. $K_{sp} = S^2$ $S = \sqrt{K_{sp}} = \sqrt{8 \times 10^{-28}} = 2\sqrt{2} \times 10^{-14}$ $= 2.82 \times 10^{-14}$ $= 282 \times 10^{-16}$ Ans. = 282
- 7. The reaction between X and Y is first order with respect to X and zero order with respect to Y.

Experiment	$\frac{[X]}{molL^{-1}}$	$\frac{[Y]}{molL^{-1}}$	$\frac{\text{Initial rate}}{\text{mol } L^{-1} \text{ min}^{-1}}$
I.	0.1	0.1	2×10^{-3}
II.	L	0.2	4×10^{-3}
III.	0.4	0.4	$M \times 10^{-3}$
IV.	0.1	0.2	2×10^{-3}

Examine the data of table and calculate ratio of numerical values of M and L. (Nearest Inetger)

Official Ans. by NTA (40)

Sol. $r = k [x] [y]^{0} = k [x]$ Using I & II $\frac{4 \times 10^{-3}}{2 \times 10^{-3}} = \left(\frac{L}{0.1}\right) \Rightarrow L = 0.2$ Using I & III $\frac{M \times 10^{-3}}{2 \times 10^{-3}} = \frac{0.4}{0.1} \Rightarrow M = 8$ $\frac{M}{L} = \frac{8}{0.2} = 40$ Ans. 40 8. In a linear tetrapeptide (Const

In a linear tetrapeptide (Constituted with different amino acids), (number of amino acids) - (number of peptide bonds) is _____.

Official Ans. by NTA (1)

Sol. In Tetrapeptide,

No. of Amino Acids = 4 No. of Peptide bonds = 3 Hence Ans. = 1

9. In bromination of Propyne, with Bromine 1, 1, 2, 2-tetrabromopropane is obtained in 27% yield. The amount of 1, 1, 2, 2 tetrabromopropane obtained from 1 g of Bromine in this reaction is _____ × 10⁻¹ g. (Nearest integer)

(Molar Mass : Bromine = 80 g/mol)

Official Ans. by NTA (3)

Sol.
$$CH_3 - C \equiv CH + 2Br_2 \rightarrow CH_3 - \begin{array}{c} Br & Br \\ | & | \\ -C - CH \\ | & | \\ Br & Br \end{array}$$

$$= \frac{1}{160} \times \frac{1}{2} \times 360 \times 0.27$$

= 0.30375
= 3.0375 × 10⁻¹

IFe(CN)₆]³⁻ should be an inner orbital complex.
 Ignoring the pairing energy, the value of crystal field stabilization energy for this complex is (-)

 Δ_{0} . (Nearest integer)

Official Ans. by NTA (2)

Sol. $[Fe(CN)_6]^{3-}$

 $\mathrm{CN}^{\!-}\xspace$ is strong field ligand

$$\mathrm{Fe}^{+3}$$
 $\mathrm{3d}^5$ (t_{2g}^5 e_g^0)

$$3d^{5}$$

CFSE = 5 (-0.4 Δ_0) = -2.0 Δ_0

Ans. (2)



FINAL JEE-MAIN EXAMINATION - JULY, 2022 (Held On Friday 29th July, 2022) TIME: 9:00 AM to 12:00 NOON MATHEMATICS TEST PAPER WITH SOLUTION **SECTION-A** Sol. $AB = 0 \Rightarrow |AB| = 0$ 1. Let R be a relation from the set $\{1, 2, 3, \dots, 60\}$ |A| |B| = 0to itself such that $R = \{(a, b) : b = pq, where$ |A| = 0|B| = 0p, $q \ge 3$ are prime numbers}. Then, the number of If $|A| \neq 0$, B = 0 (not possible) elements in R is : If $|B| \neq 0$, A = 0 (not possible) (A) 600 (B) 660 Hence $|\mathbf{A}| = |\mathbf{B}| = 0$ \Rightarrow AX = 0 has infinitely many solutions (C) 540 (D) 720 $\frac{1}{(20-a)(40-a)} + \frac{1}{(40-a)(60-a)} + \dots +$ 4. Official Ans. by NTA (B) $\frac{1}{(180 - a)(200 - a)} = \frac{1}{256}$, then the maximum value **Sol.** Number of possible values of a = 60, for b = pq, of a is : (A) 198 (B) 202 If p = 3, q = 3, 5, 7, 11, 13, 17, 19 (C) 212 (D) 218 If p = 5 q = 5, 7, 11Official Ans. by NTA (C) If p = 7 q = 7Total cases = $60 \times 11 = 660$ Sol. By splitting If z = 2 + 3i, then $z^{5} + (\overline{z})^{5}$ is equal to : 2. $\frac{1}{20}\left[\left(\frac{1}{20-a}-\frac{1}{40-a}\right)+\left(\frac{1}{40-a}-\frac{1}{60-a}\right)\right]$ (A) 244 (B) 224 (C) 245 (D) 265 $+...+\left(\frac{1}{180-a}-\frac{1}{200-a}\right)$ Official Ans. by NTA (A) $\Rightarrow \frac{1}{20} \left(\frac{1}{20-a} - \frac{1}{200-a} \right) = \frac{1}{256}$ **Sol.** $z^5 + (\overline{z})^5 = (2+3i)^5 + (2-3i)^5$ $(20 - a) (200 - a) = 256 \times 9$ $= 2({}^{5}C_{0}2^{5} + {}^{5}C_{2}2^{3}(3i)^{2} + {}^{5}C_{4}2^{1}(3i)^{4})$ $a^2 - 220a + 1696 = 0$ $= 2 (32 + 10 \times 8 (-9) + 5 \times 2 \times 81) = 244$ a = 8, 212 Let A and B be two 3×3 non-zero real matrices 3. Hence maximum value of a is 212. such that AB is a zero matrix. Then If $\lim_{x\to 0} \frac{\alpha e^x + \beta e^{-x} + \gamma \sin x}{r \sin^2 x} = \frac{2}{3},$ 5. (A) The system of linear equations AX = 0 has a unique solution where $\alpha, \beta, \gamma \in \mathbb{R}$, then which of the following is (B) The system of linear equations AX = 0 has NOT correct ? infinitely many solutions $(A) \alpha^2 + \beta^2 + \gamma^2 = 6$ (C) B is an invertible matrix (B) $\alpha\beta + \beta\gamma + \gamma\alpha + 1 = 0$ (D) adj (A) is an invertible matrix (C) $\alpha\beta^2 + \beta\gamma^2 + \gamma\alpha^2 + 3 = 0$ Official Ans. by NTA (B) (D) $\alpha^2 - \beta^2 + \gamma^2 = 4$ Official Ans. by NTA (C)



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7.

$$\lim_{x \to 0} \frac{\alpha \left(1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots\right) + \beta \left(1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots\right) + \gamma \left(x - \frac{x^3}{3!} + \dots\right)}{x^3}$$

constant terms should be zero

 $\Rightarrow a + \beta = 0$

coeff of x should be zero

 $\Rightarrow \alpha - \beta + \gamma = 0$

coeff of x^2 should be zero

$$\lim_{x \to 0} \frac{x^3 \left(\frac{\alpha}{3!} - \frac{\beta}{3!} - \frac{\gamma}{3!}\right) + x^4 \left(\frac{\alpha}{3!} - \frac{\beta}{3!} - \frac{\gamma}{3!}\right)}{x^3} = \frac{1}{3}$$

$$\Rightarrow \frac{\alpha}{2} + \frac{\beta}{2} = 0$$

$$\frac{\alpha}{6} - \frac{\beta}{6} - \frac{\gamma}{6} = \frac{2}{3}$$

$$\Rightarrow \alpha = 1, \beta = -1, \gamma = -2$$

The integral $\int_{0}^{\frac{\pi}{2}} \frac{1}{3 + 2\sin x + \cos x} dx$ is equal to:

(B) $\tan^{-1}(2) -$

(C) $\frac{1}{2} \tan^{-1}(2) - \frac{\pi}{8}$ (D) $\frac{1}{2}$

(A) $\tan^{-1}(2)$

Official Ans. by NTA (B)

Sol.

6.

$$I = \int_{0}^{\frac{\pi}{2}} \frac{dx}{3 + 2\sin x + \cos x} = \int_{0}^{\frac{\pi}{2}} \frac{\sec^{2} \frac{x}{2} dx}{2\tan^{2} \frac{x}{2} + 4\tan \frac{x}{2} + 4}$$

Put $\tan \frac{x}{2} = t$, so

$$I = \int_{0}^{1} \frac{dt}{(t+1)^{2} + 1} = \tan^{-1} (x+1) \Big|_{0}^{1} = \tan^{-1} 2 - \frac{\pi}{4}$$

Let the solution curve y = y(x) of the differential equation $(1 + e^{2x}) \left(\frac{dy}{dx} + y\right) = 1$ pass through the point $\left(0, \frac{\pi}{2}\right)$. Then, $\lim_{x \to \infty} e^x y(x)$ is equal to : (A) $\frac{\pi}{4}$ (B) $\frac{3\pi}{4}$ (C) $\frac{\pi}{2}$ (D) $\frac{3\pi}{2}$ Official Ans. by NTA (B)

Sol.
$$\frac{dy}{dx} + y = \frac{1}{1 + e^{2x}}$$

So integrating factor is $e^{\int 1.dx} = e^x$

So solution is
$$y \cdot e^x = \tan^{-1}(e^x) + c$$

Now as curve is passing through
$$\left(0, \frac{\pi}{2}\right)$$
 so

$$\Rightarrow \lim_{x \to \infty} (y \cdot e^x) = \lim_{x \to \infty} (\tan^{-1}(e^x) + \frac{\pi}{4}) = \frac{3\pi}{4}$$

Let a line L pass through the point of intersection of the lines bx + 10y - 8 = 0 and 2x - 3y = 0, $b \in R - \left\{\frac{4}{3}\right\}$. If the line L also passes through the point (1, 1) and touches the circle 17 (x² + y²) = 16, then the eccentricity of the ellipse $\frac{x^2}{5} + \frac{y^2}{b^2} = 1$ is :

(A)
$$\frac{2}{\sqrt{5}}$$
 (B) $\sqrt{\frac{3}{5}}$
(C) $\frac{1}{\sqrt{5}}$ (D) $\sqrt{\frac{2}{5}}$

Official Ans. by NTA (B)

Sol. Line is passing through intersection of bx + 10y - 8 = 0 and 2x - 3y = 0 is $(bx + 10y - 8) + \lambda(2x - 3y) = 0$. As line is passing through (1,1) so $\lambda = b + 2$

8.

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Now line (3b+4)x - (3b-4)y - 8 = 0 is tangent to circle $17(x^2 + y^2) = 16$

So
$$\frac{8}{\sqrt{(3b+4)^2 + (3b-4)^2}} = \frac{4}{\sqrt{17}}$$

 $\Rightarrow b^2 = 2 \Rightarrow e = \sqrt{\frac{3}{5}}$

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9. If the foot of the perpendicular from the point A(-1, 4, 3) on the plane P : 2x + my + nz = 4, is $\left(-2, \frac{7}{2}, \frac{3}{2}\right)$, then the distance of the point A from the plane P, measured parallel to a line with direction ratios 3, -1, -4, is equal to :

(A) 1 (B) $\sqrt{26}$ (C) $2\sqrt{2}$ (D) $\sqrt{14}$

Official Ans. by NTA (B)

Sol.

$$A(-1,4,3)$$

C B (3,-1,-4)

Let B be foot of \perp coordinates of $B = \left(-2, \frac{7}{2}, \frac{3}{2}\right)$ Direction ratio of line AB is < 2, 1, 3 >so m = 1, n = 3So equation of AC is $\frac{x+1}{3} = \frac{y-4}{-1} = \frac{z-3}{-4} = \lambda$ So point C is $(3\lambda - 1, -\lambda + 4, -4\lambda + 3)$. But C lies on the plane, so $6\lambda - 2 - \lambda + 4 - 12\lambda + 9 = 4$ $\Rightarrow \lambda = 1 \Rightarrow C(2, 3, -1)$ $\Rightarrow AC = \sqrt{26}$

10. Let
$$a = 3i + j$$
 and $b = i + 2j + k$. Let c be
a vector satisfying $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{b} + \lambda \vec{c}$. If
 \vec{b} and \vec{c} are non-parallel, then the value of λ is :
(A) -5 (B) 5
(C) 1 (D) - 1
Official Ans. by NTA (A)
Sol. $a = 3\hat{i} + \hat{j}, \vec{b} = \hat{i} + 2\hat{j} + \hat{k}$
As $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{b} + \lambda \vec{c}$
 $\Rightarrow \vec{a} \cdot \vec{c} = 1, \vec{a} \cdot \vec{b} = -\lambda$
 $\Rightarrow (3\hat{i} + \hat{j}) \cdot (\hat{i} + 2\hat{j} + \hat{k}) = -\lambda$
 $\Rightarrow \lambda = -5$
11. The angle of elevation of the top of a tower from a

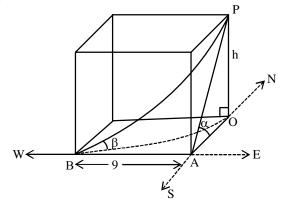
1. The angle of elevation of the top of a tower from a point A due north of it is α and from a point B at a distance of 9 units due west of A is $\cos^{-1}\left(\frac{3}{\sqrt{13}}\right)$. If the distance of the point B from the

tower is 15 units, then $\cot \alpha$ is equal to :

(A)
$$\frac{6}{5}$$
 (B) $\frac{9}{5}$
(C) $\frac{4}{3}$ (D) $\frac{7}{3}$

Official Ans. by NTA (A)





```
given OB = 15

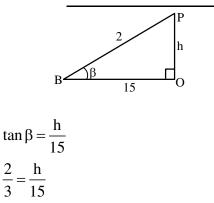
\cos \beta = \frac{3}{\sqrt{13}}
\beta
\beta
3
```

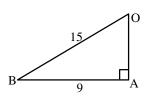
$$\tan\beta = \frac{2}{3}$$



10 = h

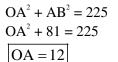
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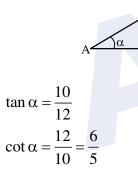




10

12





12. The statement $(p \land q) \Rightarrow (p \land r)$ is equivalent to : (A) $q \Rightarrow (p \land r)$ (B) $p \Rightarrow (p \land r)$ (C) $(p \land r) \Rightarrow (p \land q)$ (D) $(p \land q) \Rightarrow r$ Official Ans. by NTA (D)

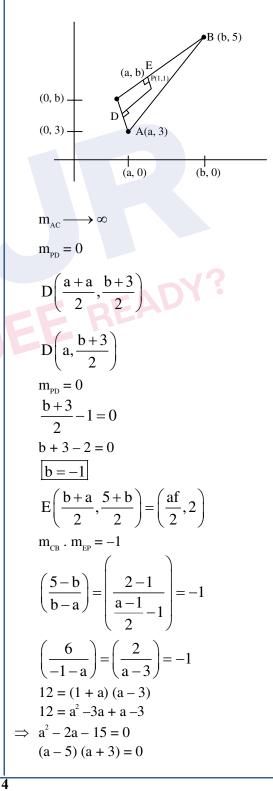
Sol.
$$(p \land q) \Rightarrow (p \land r)$$

 $\sim (p \land q) \lor (p \land r)$
 $(\sim p \lor \sim q) \lor (p \land r)$
 $(\sim p \lor (p \land r)) \lor \sim q$
 $(\sim p \lor p) \land (\sim p \lor r) \lor \sim q$
 $(\sim p \lor r) \lor \sim q$
 $(\sim p \lor \sim q) \lor r$
 $\sim (p \land q) \lor r$
 $(p \land q) \Rightarrow r$

13. Let the circumcentre of a triangle with vertices A(a, 3), B(b, 5) and C(a, b), ab > 0 be P(1, 1). If the line AP intersects the line BC at the point Q(k₁, k₂), then k₁ + k₂ is equal to :

(A) 2 (B)
$$\frac{4}{7}$$
 (C) $\frac{2}{7}$ (D) 4

Official Ans. by NTA (B)



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a = 5 or a = -3Given ab > 0a(-1) > 0-a > 0a < 0 |a = -3| Accept AP line A (-3, 3) P(1, 1) $y-1 = \left(\frac{3-1}{-3-1}\right)(x-1)$ -2y + 2 = x - 1 \Rightarrow x + 2y = 3 Appling(1) Line BC B(-1, 5)C(-3, -1) $\left(y-5\right) = \frac{6}{2}(x+1)$ y - 5 = 3x + 3y = 3x + 8.....(2) Solving (1) & (2) x + 2(3x + 8) = 3 \Rightarrow 7x + 16 = 3 7x = -13 $\mathbf{x} = -\frac{13}{7}$ $y = 3\left(-\frac{13}{7}\right) + 8$ AREYOU $=\frac{-39+56}{7}$ $y = \frac{17}{7}$ $x + y = \frac{-13 + 17}{7} = \frac{4}{7}$

14. Let \hat{a} and \hat{b} be two unit vectors such that the angle between them is $\frac{\pi}{4}$. If θ is the angle between the vectors $(\hat{a} + \hat{b})$ and $(\hat{a} + 2\hat{b} + 2(\hat{a} \times \hat{b}))$, then the value of 164 cos² θ is equal to : (A) 90 + 27 $\sqrt{2}$ (B) 45 + 18 $\sqrt{2}$ (C) 90 + $3\sqrt{2}$ (D) 54 + 90 $\sqrt{2}$ Official Ans. by NTA (A)

Sol.
$$\hat{a} \wedge \hat{b} = \frac{\pi}{4} = \phi$$

 $\hat{a} \cdot \hat{b} = |\hat{a}| |\hat{b}| \cos \phi$
 $\hat{a} \cdot \hat{b} = \cos \phi = \frac{1}{\sqrt{2}}$
 $\cos \theta = \frac{(\hat{a} + \hat{b}) \cdot (\hat{a} + 2\hat{b} + 2(\hat{a} \times \hat{b}))}{|\hat{a} + \hat{b}|^2 = (\hat{a} + \hat{b}) \cdot (\hat{a} + \hat{b})}$
 $|\hat{a} + \hat{b}|^2 = (\hat{a} + \hat{b}) \cdot (\hat{a} + \hat{b})$
 $|\hat{a} + \hat{b}|^2 = 2 + 2\hat{a} \cdot \hat{b}$
 $= 2 + \sqrt{2}$
 $\hat{a} \times \hat{b} = |\hat{a}| |\hat{b}| \sin \phi \hat{n}$
 $\hat{a} \times \hat{b} = \frac{\hat{n}}{\sqrt{2}}$ when \hat{n} is vector \bot \hat{a} and \hat{b}
let $\vec{c} = \hat{a} \times \hat{b}$
We know.
 $\vec{c} \cdot \vec{a} = 0$
 $\vec{c} \cdot \vec{b} = 0$
 $|\hat{a} + 2\hat{b} + 2\hat{c}|^2$
 $= 1 + 4 + \frac{(4)}{2} + 4 \hat{a} \cdot \hat{b} + 8\hat{b} \cdot \vec{c} + 4\vec{c} \cdot \hat{a}$
 $= 7 + \frac{4}{\sqrt{2}} = 7 + 2 \sqrt{2}$
Now
 $(\hat{a} + \hat{b}) \cdot (\hat{a} + 2\hat{b} + 2\hat{c})$
 $= |\hat{a}|^2 + 2\hat{a} \cdot \hat{b} + 0 + \hat{b} \cdot \hat{a} + 2|\hat{b}|^2 + 0$
 $= 1 + \frac{2}{\sqrt{2}} + \frac{1}{\sqrt{2}} + 2$
 $= 3 + \frac{3}{\sqrt{2}}$
 $\cos^2 \theta = \frac{3 + \frac{3}{\sqrt{2}}}{2(2 + \sqrt{2})(7 + 2\sqrt{2})}$



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$$\cos^{2} \theta = \left(\frac{9}{2\sqrt{2}}\right) \frac{\left(\sqrt{2}+1\right)}{\left(7+2\sqrt{2}\right)}$$

$$164 \cos^{2} \theta = \frac{(82)(9)}{\sqrt{2}} \frac{\left(\sqrt{2}+1\right)}{\left(7+2\sqrt{2}\right)} \frac{\left(7-2\sqrt{2}\right)}{\left(7-2\sqrt{2}\right)}$$

$$= \frac{(82)}{\sqrt{2}} \frac{\left(9\right) \left[7\sqrt{2}-4+7-2\sqrt{2}\right]}{(41)}$$

$$= \left(9\sqrt{2}\right) \left[5\sqrt{2}+3\right]$$

$$= 90 + 27\sqrt{2}$$

15. If f (\alpha) =
$$\int_{1}^{\alpha} \frac{\log_{10} t}{1+t} dt, \alpha > 0$$
, then f (e³) + f (e⁻³)

is equal to :

(A) 9
(B)
$$\frac{9}{2}$$

(C) $\frac{9}{\log_{e}(10)}$
(D) $\frac{9}{2\log_{e}(10)}$

Official Ans. by NTA (D)

Sol.
$$f(e^{3}) = \int_{1}^{e^{3}} \frac{\ln t}{\ln 10(1+t)} dt \dots (1)$$
$$f(\alpha) = \int_{1}^{\alpha} \frac{\ln t}{(\ln 10)(1+t)} dt$$
$$t = \frac{1}{x} \Rightarrow x = \frac{1}{t}$$
$$dt = -\frac{1}{x^{2}} dx$$
$$= \int_{1}^{\frac{1}{\alpha}} \frac{-\ln x}{(\ln 10)(1+\frac{1}{x})} \left(-\frac{1}{x^{2}}\right) dx$$
$$f(\alpha) = \frac{1}{\ln 10} \int_{1}^{\frac{1}{\alpha}} \frac{\ln x}{x(x+1)} dx$$
$$f(e^{-3}) = \frac{1}{\ln 10} \int_{1}^{e^{3}} \frac{\ln t}{t(t+1)} dt \dots (2)$$
Add (1) & (2)
$$f(e^{3}) + f(e^{-3})$$
$$= \left(\frac{1}{(\ln 10)}\right) \int_{1}^{e^{3}} \frac{\ln t}{t} dt$$
$$= \left(\frac{1}{(\ln 10)}\right) \int_{1}^{3} \frac{\ln t}{t} dt$$
$$\ln t = r$$

$$\frac{dt}{t} = dr$$

$$= \frac{1}{\ell n 10} \int_{0}^{3} r dr$$

$$= \left(\frac{1}{\ell n 10}\right) \left(\frac{r^{2}}{2}\right) \Big|_{0}^{3}$$

$$= \left(\frac{1}{\ell n 10}\right) \left(\frac{9}{2}\right)$$

$$= \frac{9}{2 \log_{e} 10}$$
16. The area of the region
$$\left\{ (x, y) : |x - 1| \le y \le \sqrt{5 - x^{2}} \right\} \text{ is equal to :}$$

$$(A) \frac{5}{2} \sin^{-1} \left(\frac{3}{5}\right) - \frac{1}{2} \qquad (B) \frac{5\pi}{4} - \frac{3}{2}$$

$$(C) \frac{3\pi}{4} + \frac{3}{2} \qquad (D) \frac{5\pi}{4} - \frac{1}{2}$$

Official Ans. by NTA (D)

Sol.

$$|x-1| < y < \sqrt{5-x^2}$$
When $|x-1| = \sqrt{5-x^2}$

$$\Rightarrow (x-1)^2 = 5-x^2$$

$$\Rightarrow x^2 - x - 2 = 0$$

$$\Rightarrow x = 2, -1$$

Required Area = Area of $\triangle ABC$ + Area of region BCD

$$= \frac{1}{2} \begin{vmatrix} 1 & 0 & 1 \\ 2 & 1 & 1 \\ -1 & 2 & 1 \end{vmatrix} + \frac{\pi}{4} \left(\sqrt{5}\right)^2 - \frac{1}{2} \left(\sqrt{5}\right)^2$$
$$= \frac{5\pi}{4} - \frac{1}{2}$$

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17. Let the focal chord of the parabola $P : y^2 = 4x$ along the line L : y = mx + c, m > 0 meet the parabola at the points M and N. Let the line L be a tangent to the hyperbola $H : x^2 - y^2 = 4$. If O is the vertex of P and F is the focus of H on the positive x-axis, then the area of the quadrilateral OMFN is :

(A) $2\sqrt{6}$ (B) $2\sqrt{14}$

(C) $4\sqrt{6}$	(D) $4\sqrt{14}$
(\mathbf{c}) · \mathbf{v}	(2)

Official Ans. by NTA (B)

$$(0,0) O (0,0) O (0,0$$

Sol.

O(0.0)H: $\frac{x^2}{4} - \frac{y^2}{4} = 1$ Focus (ae, 0) $F(2\sqrt{2},0)$ Line L : y = mx + c pass (1,0) |o = m + C|(1) Line L is tangent to Hyperbola. $\frac{x^2}{4} - \frac{y^2}{4} = 1$ $C = \pm \sqrt{a^2 m^2 - \ell^2}$ $C = \pm \sqrt{4m^2 - 4}$ From (1) $-m = \pm \sqrt{4m^2 - 4}$ Squaring $m^2 = 4m^2 - 4$ $4 = 3m^{2}$ $\frac{2}{\sqrt{3}}$ = m | (as m > 0)C = -m $C = \frac{-2}{\sqrt{3}}$

$$y = \frac{2x}{\sqrt{3}} - \frac{2}{\sqrt{3}}$$

$$y^{2} = 4x$$

$$\Rightarrow \left(\frac{2x-2}{\sqrt{3}}\right)^{2} = 4x$$

$$\Rightarrow x^{2} + 1 - 2x = 3x$$

$$\Rightarrow \boxed{x^{2} - 5x + 1 = 0}$$

$$y^{2} = 4\left(\frac{\sqrt{3}y + 2}{2}\right)$$

$$y^{2} = 2\sqrt{3}y + 4$$

$$\Rightarrow \boxed{y^{2} - 2\sqrt{3}y - 4 = 0}$$

Area

$$\left|\frac{1}{2}\begin{vmatrix} 0 & x_{1} & 2\sqrt{2} & x_{2} & 0 \\ 0 & y_{1} & 0 & y_{2} & 0 \end{vmatrix}\right|$$

$$= \left|\frac{1}{2}\left[-2\sqrt{2}y_{1} + 2\sqrt{2}y_{2}\right]\right|$$

$$= \sqrt{2}\left|y_{2} - y_{1}\right| = \frac{(\sqrt{2})\sqrt{12 + 16}}{111}$$

$$= \sqrt{56}$$

$$= 2\sqrt{14}$$

- 18. The number of points, where the function $f: \mathbf{R} \rightarrow \mathbf{R}$, $f(x) = |x - 1| \cos |x - 2| \sin |x - 1| + (x - 3) |x^2 - 5x + 4|$, is NOT differentiable, is : (A) 1 (B) 2 (C) 3 (D) 4 Official Ans. by NTA (B)
- Sol. $f(x) = |x 1| \cos |x 2| \sin |x 1| + (x 3)| x^2 5x$ + 4| = |x - 1| cos |x - 2| sin |x - 1| + (x - 3)| x - 1||x - 4| = |x - 1| [cos |x - 2| sin |x - 1| + (x - 3) |x - 4|] Non differentiable at x = 1 and x = 4.
- 19. Let S = {1, 2, 3, ..., 2022}. Then the probability, that a randomly chosen number n from the set S such that HCF (n, 2022) = 1, is :

$(A)\frac{128}{1011}$	(B) $\frac{166}{1011}$
(127)	(D) $\frac{112}{112}$

(C)
$$\frac{127}{337}$$
 (D) $\frac{112}{337}$

Official Ans. by NTA (D)



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Official Ans. by NTA (D)

Sol.

Sol. Total number of elements = 2022 $2022 = 2 \times 3 \times 337$ HCF (n, 2022) = 1is feasible when the value of 'n' and 2022 has no common factor. A = Number which are divisible by 2 from $\{1,2,3,\ldots,2022\}$ n(A) = 1011B = Number which are divisible by 3 by 3 from {1,2,3.....2022} n(B) = 674 $A \cap B$ = Number which are divisible by 6 from {1,2,3.....2022} 6,12,18....., 2022 $|337 = n(A \cap B)|$ $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ = 1011 + 674 - 337= 1348C= Number which divisible by 337from {1,.....1022} C= {337,674,1011,1348,1685,20222} Already Already Already counted in counted in counted in Set $(A \cup B)$ Set $(A \cup B)$ Set $(A \cup B)$ Total elements which are divisible by 2 or 3 or 337 = 1348 + 2 = 1350Favourable cases = Element which are neither divisible by 2, 3 or 337 = 2022 - 1350= 672Required probability = $\frac{672}{2022} = \frac{112}{337}$ Let $f(x) = 3^{(x^2-2)^3+4}$, $x \in \mathbf{R}$. Then which of the 20. following statements are true ? P: x = 0 is a point of local minima of f Q : x = $\sqrt{2}$ is a point of inflection of f R : f' is increasing for x > $\sqrt{2}$ (A) Only P and Q (B) Only P and R (C) Only Q and R (D) All, P, Q and R

 $f(x) = 81.3^{(x^2-2)^3}$ $f'(x) = 81.3^{(x^2-2)^3} \cdot \ell n 3.3 (x^2-2)^2 \cdot 2x$ = $(81 \times 6)3^{(x^2-2)^3} x (x^2-2)^2 ln3$ x = 6 is point of local min $f'(x) = \underbrace{(486.\ell n3)}_{k} \underbrace{3^{(x^2-2)^3} x (x^2-2)^2}_{g(x)}$ $g'(x) = 3^{(x^2-2)^3} (x^2-2)^2 + x \cdot 3^{(x^2-2)^3} \cdot 4x \cdot (x^2-2)$ $+x.(x^{2}-2)^{2}.3^{(x^{2}-2)^{3}} ln 3.3(x^{2}-2)^{2}.2x$ $=3^{(x^{2}-2)^{3}}(x^{2}-2)\left[x^{2}-2+4x^{2}+6x^{2}\ln 3(x^{2}-2)^{3}\right]$ $g'(x) = 3^{(x^2-2)^3} (x^2-2) \left[5x^2 - 2 + 6x^2 \ln 3 (x^2-2)^3 \right]$ f''(x) = k.g'(x) $f''(\sqrt{2}) = 0, f''(\sqrt{2}^+) > 0, f''(\sqrt{2}^-) < 0$ $x = \sqrt{2}$ is point of inflection

f''(x) > 0 for $x > \sqrt{2}$ so f'(x) is increasing

SECTION-B

1. Let $S = \{\theta \in (0, 2\pi) : 7 \cos^2 \theta - 3 \sin^2 \theta - 2 \cos^2 2\theta = 2\}$. Then, the sum of roots of all the equations $x^2 - 2 (\tan^2 \theta + \cot^2 \theta) x + 6 \sin^2 \theta = 0 \theta \in S$, is_____.

Official Ans. by NTA (16)

Sol. $7\cos^2\theta - 3\sin^2\theta - 2\cos^22\theta = 2$ $4\cos^2\theta + 3\cos2\theta - 2\cos^22\theta = 2$ $2(1 + \cos 2\theta) + 3\cos 2\theta - 2\cos^22\theta = 2$ $2\cos^22\theta - 5\cos2\theta = 0$ $\cos2\theta (2\cos2\theta - 5) = 0$ $\cos2\theta = 0$

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 $2\theta = (2n + 1)\frac{\pi}{2}$ $\theta = (2n + 1)\frac{\pi}{4}$ $S = \left\{\frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}\right\}$ For all four values of θ $x^{2} - 2$ ($\tan^{2}\theta + \cot^{2}\theta$) $x + 6\sin^{2}\theta = 0$ $\Rightarrow x^{2} - 4x + 3 = 0$ Sum of roots of all four equations = $4 \times 4 = 16$.

2. Let the mean and the variance of 20 observations $x_1, x_2, ..., x_{20}$ be 15 and 9, respectively. For $\alpha \in \mathbb{R}$, if the mean of $(x_1 + \alpha)^2$, $(x_2 + \alpha)^2$, ..., $(x_{20} + \alpha)^2$ is 178, then the square of the maximum value of α is equal to _____.

Official Ans. by NTA (4)

Sol. $\sum x_{1} = 15 \times 20 = 300 \quad ...()$ $\frac{\sum x_{1}^{2}}{20} - (15)^{2} = 9 \quad ...(ii)$ $\sum x_{1}^{2} = 234 \times 20 = 4680$ $\frac{\sum (x_{1} + \alpha)^{2}}{20} = 178 \Rightarrow \sum (x_{1} + \alpha)^{2} = 3560$ $\Rightarrow \sum x_{1}^{2} + 2\alpha \sum x_{1} + \sum \alpha^{2} = 3560$ $4680 + 600\alpha + 20\alpha^{2} = 3560$ $\Rightarrow \alpha^{2} + 30\alpha + 56 = 0$ $\Rightarrow (\alpha + 28)(\alpha + 2) = 0$ $\alpha = -2, -28$ Square of maximum value of α is 4

3. Let a line with direction ratios a, -4a, -7 be perpendicular to the lines with direction ratios 3, -1, 2b and b, a, -2. If the point of intersection of the line $\frac{x+1}{a^2+b^2} = \frac{y-2}{a^2-b^2} = \frac{z}{1}$ and the plane x - y + z = 0 is (α, β, γ) , then $\alpha + \beta + \gamma$ is equal to

Sol.
$$(a,-4a,-7) \perp \text{ to } (3,-1,2b)$$

 $a = 2b$...(i)
 $(a,-4a,-7) \perp \text{ to } (b,a,-2)$
 $3a + 4a - 14b = 0$
 $ab - 4a^2 + 14 = 0$ (ii)
From Equations (i) and (ii)
 $2b^2 - 16b^2 + 14 = 0$
 $b^2 = 1$
 $a^2 = 4b^2 = 4$
 $\frac{x+1}{5} = \frac{y-2}{3} = \frac{z}{1} = k$
 $\alpha = 5k - 1, \beta = 3k + 2, \gamma = k$
As (α, β, γ) satisfies $x - y + z = 0$
 $5k - 1 - (3k + 2) + k = 0$
 $k = 1$
 $\therefore \alpha + \beta + \gamma = 9k + 1 = 10$
4 Let a, a, α be an A P. If $\sum_{r=1}^{\infty} \frac{a_r}{r} = 4$ th

4. Let $a_1, a_2, a_3,...$ be an A.P. If $\sum_{r=1}^{r} \frac{a_r}{2^r} = 4$, then $4a_2$ is equal to _____.

Official Ans. by NTA (16)

Sol.
$$S = \frac{a_1}{2} + \frac{a_2}{2^2} + \frac{a_3}{2^3} + \dots$$
$$\frac{S}{2} = \frac{a_1}{2^2} + \frac{a_2}{2^3} + \dots$$
$$\frac{S}{2} = \frac{a_1}{2} + d\left(\frac{1}{2^2} + \frac{1}{2^3} + \dots\right)$$
$$\frac{S}{2} = \frac{a_1}{2} + d\left(\frac{1}{4} - \frac{1}{2}\right)$$
$$\therefore S = a_1 + d = a_2 = 4$$
Or $4a_2 = 16$

5. Let the ratio of the fifth term from the beginning to the fifth term from the end in the binomial

expansion of $\left(\frac{4}{\sqrt{2}} + \frac{1}{\frac{4}{\sqrt{3}}}\right)^n$, in the increasing powers of $\frac{1}{\frac{4}{\sqrt{3}}}$ be $\sqrt[4]{6}$: 1. If the sixth term from the beginning is α , then α is equal to

the beginning is $\frac{\alpha}{\sqrt[4]{3}}$, then α is equal to _____.

Official Ans. by NTA (84)

Official Ans. by NTA (10)



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Sol.
$$\frac{T_5}{T_{n-3}} = \frac{{}^n C_4 (2^{1/4})^{n-4} (3^{-1/4})^4}{{}^n C_{n-4} (2^{1/4})^4 (3^{-1/4})^{n-4}} = \frac{\sqrt[4]{6}}{1}$$
$$\Rightarrow 2^{\frac{n-8}{4}} 3^{\frac{n-8}{4}} = 6^{1/4}$$
$$\Rightarrow 6^{n-8} = 6$$
$$\Rightarrow n-8 = 1 \Rightarrow n = 9$$
$$T_6 = {}^9 C_5 (2^{1/4})^4 (3^{-1/4})^5 = \frac{84}{\sqrt[4]{3}}$$
$$\therefore \alpha = 84$$

6. The number of matrices of order 3 × 3, whose entries are either 0 or 1 and the sum of all the entries is a prime number, is_____.

Official Ans. by NTA (282)

Sol.
$$\mathbf{A} = \begin{bmatrix} \mathbf{a}_{11} & \mathbf{a}_{12} & \mathbf{a}_{13} \\ \mathbf{a}_{21} & \mathbf{a}_{22} & \mathbf{a}_{23} \\ \mathbf{a}_{31} & \mathbf{a}_{32} & \mathbf{a}_{33} \end{bmatrix} \mathbf{a}_{ij} \in \{0, 1\}$$

 $\sum a_{ij} = 2, 3, 5, 7$

Total matrix = ${}^{9}C_{2} + {}^{9}C_{3} + {}^{9}C_{5} + {}^{9}C_{7}$ = 282

- 7. Let p and p + 2 be prime numbers and let
 - $\Delta = \begin{vmatrix} p! & (p+1)! & (p+2)! \\ (p+1)! & (p+2)! & (p+3)! \\ (p+2)! & (p+3)! & (p+4)! \end{vmatrix}$

Then the sum of the maximum values of α and β ,

such that p^{α} and $(p + 2)^{\beta}$ divide Δ , is _____.

Official Ans. by NTA (4)

Sol.
$$\Delta = \begin{vmatrix} P! & (P+1)! & (P+2)! \\ (P+1)! & (P+2)! & (P+3)! \\ (P+2)! & (P+3)! & (P+4)! \end{vmatrix}$$
$$\Delta = P!(P+1)!(P+2)! \begin{vmatrix} 1 & 1 & 1 \\ P+1 & P+2 & P+3 \\ (P+2)(P+1) & (P+3)(P+2) & (P+4)(P+3) \end{vmatrix}$$
$$\Delta = 2P!(P+1)!(P+2)!$$

Which is divisible by $P^{\alpha} \& (P+2)^{\beta}$

 $\therefore \alpha = 3, \beta = 1$

Ans. 4

8. If
$$\frac{1}{2 \times 3 \times 4} + \frac{1}{3 \times 4 \times 5} + \frac{1}{4 \times 5 \times 6} + \dots + \frac{1}{100 \times 101 \times 102} = \frac{k}{101}$$
, then 34 k is equal to

Sol.
$$\frac{1}{2.3.4} + \frac{1}{3.4.5} + \dots + \frac{1}{100.101.102} = \frac{k}{101}$$

 $\frac{4-2}{2.3.4} + \frac{5-3}{3.4.5} + \dots + \frac{102-100}{100.101.102} = \frac{2k}{101}$
 $\frac{1}{2.3} - \frac{1}{3.4} + \frac{1}{3.4} - \frac{1}{4.5} + \dots + \frac{1}{100.101} - \frac{1}{101.102} = \frac{2k}{101}$
 $\frac{1}{2.3} - \frac{1}{101.102} = \frac{2k}{101}$
 $\therefore 2k = \frac{101}{6} - \frac{1}{102}$
 $\therefore 34k = 286$
9. Let S = {4, 6, 9} and T = {9, 10, 11, ..., 1000}.

Let S = {4, 6, 9} and T = {9, 10, 11, ..., 1000}. If A = { $a_1 + a_2 + ... + a_k : k \in N, a_1, a_2, a_3, ..., a_k \in S$ }, then the sum of all the elements in the set T – A is equal to _____.

Give yourself an extra edge

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EE-Main Exam July 2022/29-07-2022/Morning Session

Official Ans. by NTA (11)

eedge

Sol. $S = \{4, 6, 9\}$ $T = \{9, 10, 11, \dots, 1000\}$

$$A\{a_1 + a_2 + \dots + a_k : K \in N\} \& a_i \in S$$

Here by the definition of set 'A'

 $A = \{a : a = 4x + 6y + 9z\}$

Except the element 11, every element of set T is of of the form 4x + 6y + 9z for some x, y, $z \in W$ \therefore T – A = {11} Ans. 11

10. $6y + \alpha = 0$ in line y = x + 1 be $c_2 : 5x^2 + 5y^2 + 10gx$ + 10fy + 38 = 0. If r is the radius of circle c_2 , then α + 6r² is equal to

Official Ans. by NTA (12)

Image of centre $c_1 \equiv (1,3)$ in x - y + 1 = 0 is given Sol. by $\frac{\mathbf{x}_1 - 1}{1} = \frac{\mathbf{y}_1 - 3}{-1} = \frac{-2(1 - 3 + 1)}{1^2 + 1^2}$ \Rightarrow x₁ = 2, y₁ = 2 \therefore Centre of circle $c_2 \equiv (2,2)$: Equation of c_2 be $x^2 + y^2 - 4x - 4y + \frac{38}{5} = 0$ Now radius of c_2 is $\sqrt{4 + 4 - \frac{38}{5}} = \sqrt{\frac{2}{5}} = r$ $(radius of c_1)^2 = (radius of c_2)^2$ $\Rightarrow 10 - \alpha = \frac{2}{5} \Rightarrow \alpha = \frac{48}{5}$ $\therefore \alpha + 6r^2 = \frac{48}{5} + \frac{12}{5} = 12$ ARE YOU JEE READY?